

Marfleet Primary Academy Calculation Policy



Introduction

This calculation policy has been produced to ensure consistency in teaching throughout the school. It provides an overview of the variety of strategies used in our school to teach arithmetic (the four operations) throughout the Primary Mathematics Curriculum.

The progression of the four operations (+ , - , X and ÷) are shown across all of the year groups, including the Early Years Foundation Stage. **Children should be taught the strategies from the appropriate year group, deepening their learning by applying, explaining and reasoning rather than moving on to the next year group objective.**

Pupils are introduced to calculation through the Concrete, Pictorial , Abstract (CPA) methods using practical, oral and mental activities. Pupils begin to become fluent in their understanding by using concrete objects and manipulatives. When they become more secure, they begin to develop ways of recording to support their thinking and calculation methods, first using pictorial methods and then moving to informal written methods and onwards to abstract, formal written calculation methods. Over time pupils will learn how to use models and images such as empty number lines, to support their mental and informal written method of calculation.

As pupils' mental methods are strengthened and refined, so too are their informal written methods. Some recording takes the form of jottings, which are used to support pupils' thinking. More formal written methods follow only when a child is secure in using a wide range of mental calculation strategies to support them.

This policy contains key concrete, pictorial and the key pencil and paper abstract procedures that will be taught in our school. It has been written to ensure consistency and progression throughout the school and reflects a whole school agreement. **Each method should be introduced using concrete and pictorial representations to support a deeper understanding of the abstract concept, with representations continually used to reinforce and underpin conceptual understanding.**

It is important that pupils do not abandon jottings and mental methods once written, formal pencil and paper procedures are introduced, until they become secure in the formal procedures. Therefore pupils will always be encouraged to look at a calculation / problem and then decide which method would be the most appropriate one to use; pictorial, with the use of manipulatives, mental calculation with jottings, or a structured formal recording. The expectation is that pupils are secure in using the most efficient method appropriate to the age related expectations for their year group.

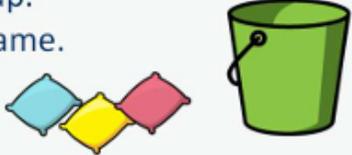
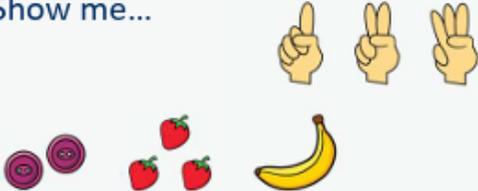
Progression of Skills - Addition

Year group	Skill
Nursery	<ul style="list-style-type: none">• Subitise to 3• Count how many• Make numbers to 5• Add 1 more (through songs and rhymes)
Reception	<ul style="list-style-type: none">• Conceptually subitise to 5• 1 more• Notice the composition of numbers within 10• Combine 2 groups• Add more
Year 1	<ul style="list-style-type: none">• Add together• Add more• Bonds within 10• Related facts within 20• Missing numbers

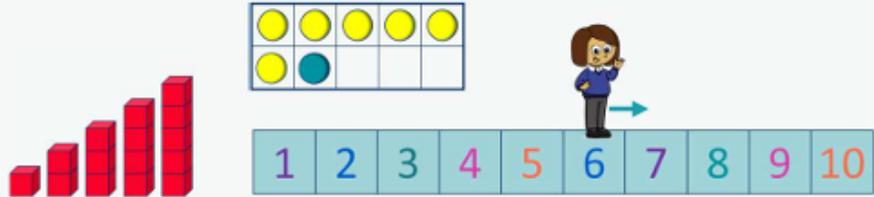
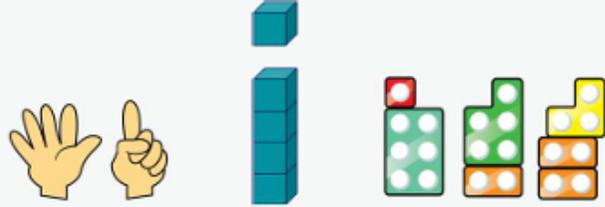
Year group	Skill
Year 2	<ul style="list-style-type: none">• Add 1s to any number (related facts)• Add three 1-digit numbers• Add across a 10• Add multiples of 10• Add 10s to any number• Add two 2-digit numbers (not across a ten)• Add two 2-digit numbers (across a ten)• Missing numbers
Year 3	<ul style="list-style-type: none">• Add 1s, 10s and 100s to a 3-digit number• Add two numbers (no exchange)• Add two numbers across a 10 or 100• Complements to 100• Add fractions with the same denominator within 1 whole• Calculate the duration of events

Year group	Skill
Year 4	<ul style="list-style-type: none">• Add 1s, 10s and 100s to a 4-digit number• Add up to two 4-digit numbers• Add decimal numbers in the context of money• Add fractions and mixed numbers with the same denominator beyond 1 whole
Year 5	<ul style="list-style-type: none">• Add using mental strategies• Add whole numbers with more than 4 digits• Add decimals with up to 2 decimal places• Complements to 1• Add fractions with denominators that are a multiple of one another
Year 6	<ul style="list-style-type: none">• Add integers up to 10 million• Add decimals with up to 3 decimal places• Order of operations• Negative numbers• Add fractions

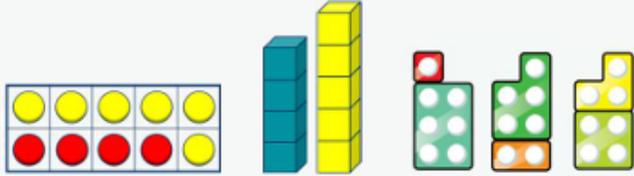
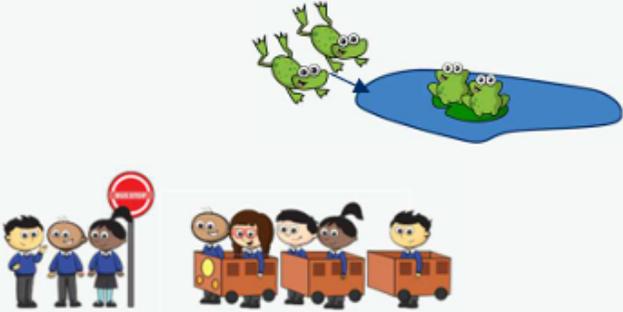
Addition - Nursery

<p>Nursery</p>	<ul style="list-style-type: none"> • Begin to have an understanding of numbers to 5 • We recommend focusing on noticing and representing small quantities, perceptual subitising and counting. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Subitise to 3</p> <p>Instantly see how many.</p>	<p>How many do you see?</p> 	
<p>Count how many</p> <p>Begin to count objects using 1-1 correspondence.</p>	<p>How many are there?</p> <p>1 2 3 4 5</p> 	<p>Count out ... from a larger group. E.g. Collect 3 beanbags for a game.</p> 
<p>Make numbers to 5</p> <p>Start by showing 1, 2 and 3 using fingers.</p>	<p>Show me...</p> 	<p>Begin to link numerals to quantities.</p> 
<p>Add 1 more</p> <p>Through stories, songs and rhymes.</p>	<p>How many do I have now?</p> 	

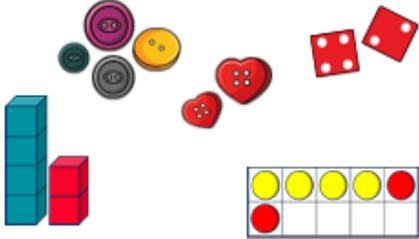
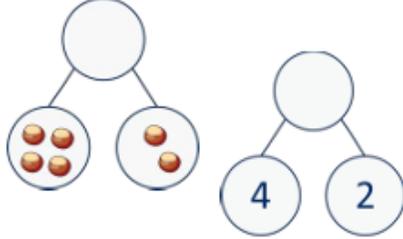
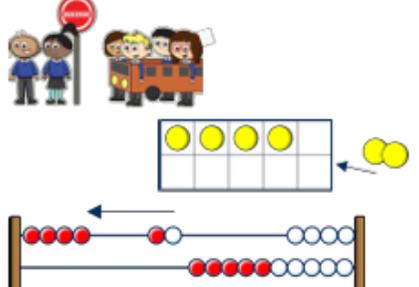
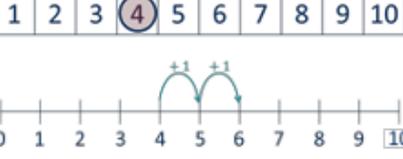
Addition - Reception

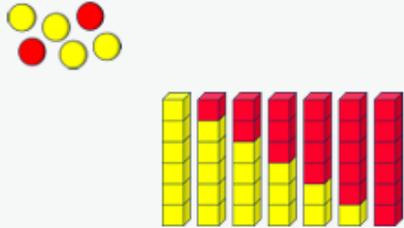
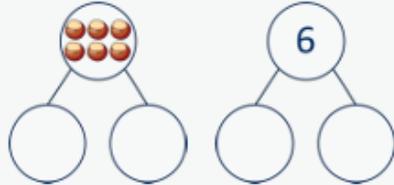
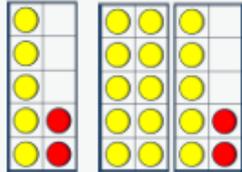
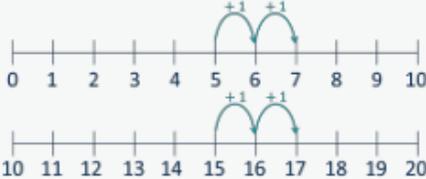
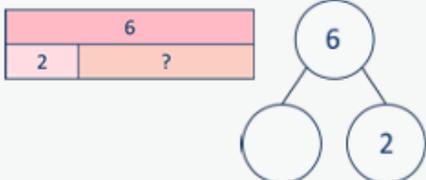
<p>Reception</p>	<ul style="list-style-type: none"> • Have a deep understanding of numbers to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Conceptually subitise to 5</p> <p>Notice the parts that make up the whole.</p>	<p>What do you see? How do you see it?</p> 	
<p>1 more</p> <p>Continue to link to stories, songs and rhymes.</p>	<p>1 more than ... is ...</p> 	
<p>Notice the composition of numbers within 10</p> <p>Link to stories, songs and rhymes.</p>	<p>How many...? How many...? How many altogether?</p> 	<p>How many ways can you make...?</p> 

Addition - Reception

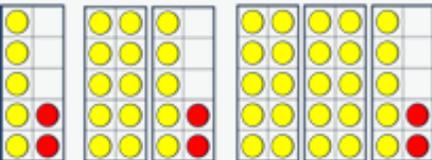
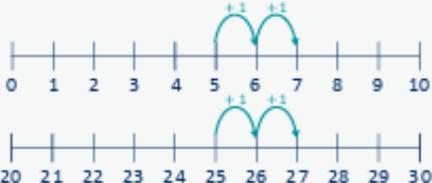
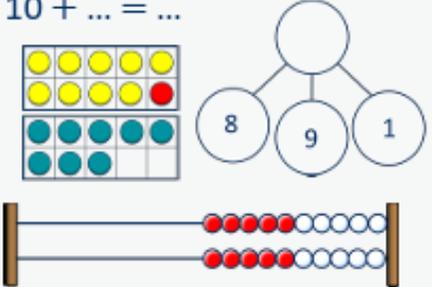
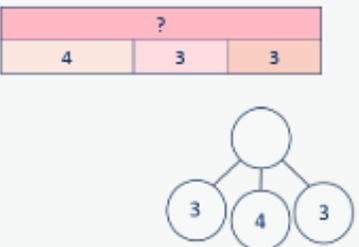
Progression of skills	Key representations	
<p>Combine 2 groups</p> <p>2 groups are combined to find the total.</p>	<p>There are There are There are altogether.</p> 	<p>.... and make</p> 
<p>Add more</p> <p>A quantity is increased.</p>	<p>First... Then.... Now....</p> 	<p>I have I add more. Now I have....</p> 

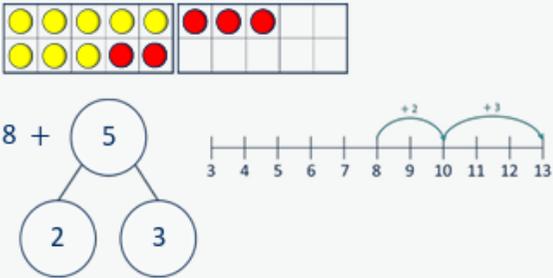
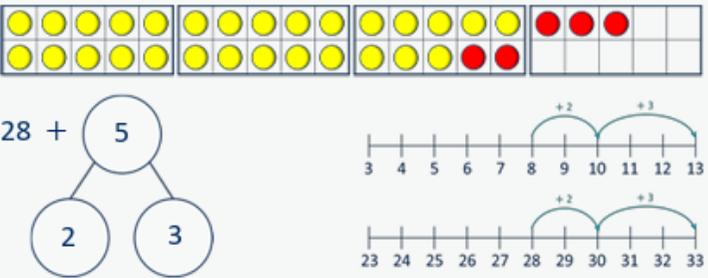
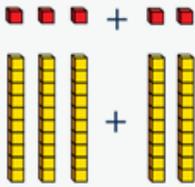
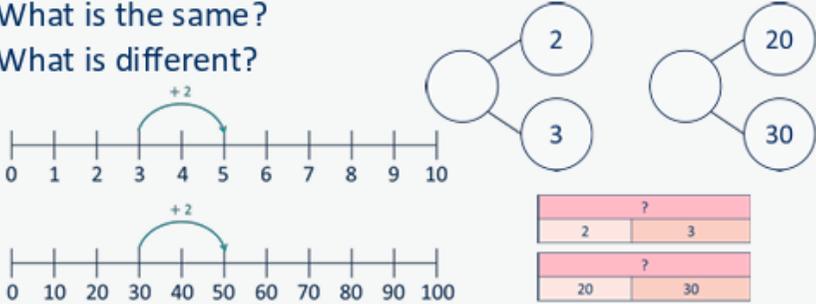
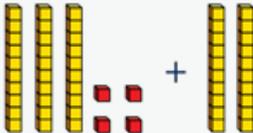
Addition - Year 1

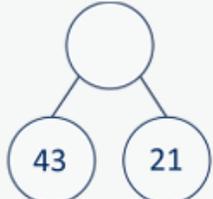
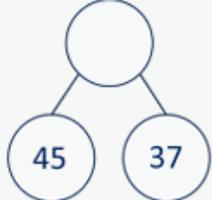
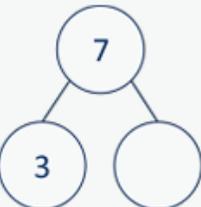
<p>Year 1</p>	<ul style="list-style-type: none"> • Read, write and interpret mathematical statements involving addition (+) and equals (=) signs. • Represent and use number bonds within 20 • Add 1-digit and 2-digit numbers to 20, including zero. • Solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as $7 = \square + 2$ 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Add together (aggregation)</p> <p>2 quantities are combined to find the total.</p>	<p>There are ... There are ... There are ... altogether.</p> 	<p>... is a part. ... is a part. ... is the whole.</p> 	<p>... plus ... is equal to is equal to ... + ...</p> $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$
<p>Add more (augmentation)</p> <p>A quantity is increased.</p>	<p>First... Then... Now...</p> 	<p>I start at ... I jump on ... I land on ...</p> 	<p>... plus ... is equal to is equal to ... + ...</p> $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$

Progression of skills	Key representations		
<p>Bonds within 10</p> <p>Include bonds for each number within 10</p> <p>Encourage children to notice patterns.</p>	<p>... is made of ... and and ... make ...</p> 	<p>... can be partitioned into ... and ...</p> 	<p>... plus ... is equal to ...</p> $6 + 0 = 6$ $5 + 1 = 6$ $4 + 2 = 6$ $3 + 3 = 6$ $2 + 4 = 6$ $1 + 5 = 6$ $0 + 6 = 6$
<p>Related facts within 20</p> <p>Make links to known facts.</p>	<p>I know that ... and ... = ... so ... and ... = ...</p> 	<p>... more than ... is ... so ... more than ... is ...</p> 	<p>What patterns do you notice?</p> $5 + 2 = 7$ $15 + 2 = 17$ $7 = 5 + 2$ $17 = 15 + 2$
<p>Missing numbers</p> <p>Make links to known facts.</p>	<p>How many more do you need to make ...?</p> 	<p>If ... is the whole and ... is a part, the other part must be...</p> 	<p>... plus ... is equal to ...</p> $2 + \square = 6$ $6 = 2 + \square$ 

Addition - Year 2

<p>Year 2</p>	<ul style="list-style-type: none"> Recall and use addition facts to 20 fluently, and derive and use related facts up to 100 Add numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> a two-digit number and 1s a two-digit number and 10s 2 two-digit numbers adding 3 one-digit numbers Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Add ones to any number (related facts)</p> <p>Make links to known facts.</p>	<p>I know that ... and ... = ... so ... and ... = ...</p> 	<p>... more than ... is ... so ... more than ... is ...</p> 	<p>What do you notice? Can you continue the pattern?</p> <p>$5 + 2 = 7$ $15 + 2 = 17$ $25 + 2 = 27...$</p>
<p>Add three 1-digit numbers</p> <p>Prompt children to understand that addition can be done in any order and to make links to known facts.</p>	<p>... and ... are a bond to 10 $10 + ... = ...$</p> 	<p>Double ... + ... = ...</p> 	<p>What do you notice? Which addition is the easiest to calculate?</p> <p>$8 + 9 + 1 =$ $8 + 1 + 9 =$ $9 + 1 + 8 =$</p>

Progression of skills	Key representations																																																													
<p>Add across a 10</p> <p>Partition the number being added to make a full ten.</p>	<p>... can be partitioned into ... and ...</p> 	<p>I add ... to get to ... then I add ...</p> $8 + 5 = 13$ $28 + 5 = 33$ 																																																												
<p>Add multiples of 10</p> <p>Make links to known facts within ten.</p>	<p>... ones + ... ones = ... ones so ... tens + ... tens = ... tens</p>  $3 + 2 = 5$ $30 + 20 = 50$	<p>What is the same? What is different?</p>  <table border="1" data-bbox="1711 831 1921 879"> <tr><td>?</td></tr> <tr><td>2</td><td>3</td></tr> </table> <table border="1" data-bbox="1711 890 1921 938"> <tr><td>?</td></tr> <tr><td>20</td><td>30</td></tr> </table>	?	2	3	?	20	30																																																						
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<p>Add 10s to any number</p> <p>Make links to known facts.</p>	<p>... tens + ... tens = ... tens ... tens and ... ones = ...</p> 	<p>To add ... I need to add 10 ... times.</p> <table border="1" data-bbox="1196 1075 1518 1262"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> </table> <p>I know that ... and ... = ... so ... and ... = ...</p> $30 + 20 = 50$ $34 + 20 = 54$	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
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Progression of skills	Key representations																																		
<p>Add 2-digit numbers (not across a ten)</p> <p>Lining up ones and tens in columns will support with later written methods.</p>	<p>... ones + ... ones = ... ones ... tens + ... tens = ... tens</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th style="background-color: #fff9c4;">Tens</th><th style="background-color: #f8bbd0;">Ones</th></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td>██</td></tr> </table> <div style="text-align: center;">  </div> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th colspan="2" style="background-color: #f8bbd0;">?</th></tr> <tr><td style="background-color: #fff9c4;">43</td><td style="background-color: #fff9c4;">21</td></tr> </table> </div> <p style="text-align: right;"> 3 ones + 1 one = 4 ones 4 tens + 2 tens = 6 tens 6 tens + 4 ones = 64 </p>			Tens	Ones	████████	██	████████	██	████████	██	████████	██	████████	██	████████	██	████████	██	?		43	21												
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<p>Add 2-digit numbers (across a ten)</p> <p>Begin to exchange 10 ones for 1 ten.</p>	<p>There are ... ones, so I do/do not need to make an exchange.</p> <p>... ones = ... ten and ... ones</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th style="background-color: #fff9c4;">T</th><th style="background-color: #f8bbd0;">O</th></tr> <tr><td>████████</td><td>██████</td></tr> <tr><td>████████</td><td>██████</td></tr> <tr><td>████████</td><td>██████</td></tr> <tr><td>████████</td><td>██████</td></tr> <tr><td>████████</td><td>██████</td></tr> <tr><td>████████</td><td>██████</td></tr> </table> → <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th style="background-color: #fff9c4;">T</th><th style="background-color: #f8bbd0;">O</th></tr> <tr><td>████████</td><td></td></tr> <tr><td>████████</td><td></td></tr> <tr><td>████████</td><td></td></tr> <tr><td>████████</td><td>██</td></tr> <tr><td>████████</td><td></td></tr> <tr><td>████████</td><td></td></tr> </table> </div> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><th colspan="2" style="background-color: #f8bbd0;">?</th></tr> <tr><td style="background-color: #fff9c4;">45</td><td style="background-color: #fff9c4;">37</td></tr> </table> <div style="text-align: center;">  </div> </div> <p style="text-align: right;"> 5 ones + 7 ones = 12 ones 12 ones = 1 ten and 2 ones 4 tens + 3 tens + 1 ten = 8 tens 8 tens and 2 ones = 82 </p>			T	O	████████	██████	████████	██████	████████	██████	████████	██████	████████	██████	████████	██████	T	O	████████		████████		████████		████████	██	████████		████████		?		45	37
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<p>Missing numbers</p> <p>Solve missing number problems and use the inverse to check.</p>	<p>How many more do you need to make ...?</p> <div style="display: flex; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>████████</td></tr> <tr><td>██</td></tr> </table> <div style="margin-left: 20px;"> $6 + \square = 10$ $10 - \square = 6$ </div> </div>	████████	██	<p>If ... is a whole and ... is a part, then ... is the other part.</p> <div style="display: flex; align-items: center;"> <div style="margin-right: 20px;"> $\square + 3 = 7$ $7 - 3 = \square$ </div> <div style="text-align: center;">  </div> </div>	<p>... can be partitioned into ... and ...</p> <p style="text-align: center;">$10 + 8 = 12 + \square$</p> <div style="display: flex; justify-content: space-around;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>████████</td></tr> <tr><td>████████</td></tr> <tr><td>████████</td></tr> <tr><td>████████</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>████████</td></tr> <tr><td>████████</td></tr> <tr><td>██</td></tr> <tr><td></td></tr> </table> </div>	████████	████████	████████	████████	████████	████████	██																							
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Addition - Year 3

<p>Year 3</p>	<ul style="list-style-type: none"> • Add numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds. • Add numbers with up to three digits, using formal written methods of columnar addition. • Add fractions with the same denominator within 1 whole. • Calculate the time taken by particular events or tasks. 																																				
<p>Progression of skills</p>	<p>Key representations</p>																																				
<p>Add 1s, 10s or 100s to a 3-digit number</p> <p>Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.</p>	<p>The ones/tens/hundreds column will increase by ...</p> <table border="1" data-bbox="683 622 1104 815"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p> $444 + 5 =$ $444 + 50 =$ $444 + 500 =$ </p> <table border="1" data-bbox="1144 622 1395 815"> <thead> <tr> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p> $777 + 2 =$ $777 + 20 =$ $777 + 200 =$ </p>	Hundreds	Tens	Ones				H	T	O				<p>What patterns do you notice?</p> <p> $235 + 3 =$ $235 + 30 =$ $235 + 300 =$ </p> <p> $111 + \square = 118$ $111 + \square = 181$ $111 + \square = 811$ </p> <p> $604 + 20 =$ $604 + 50 =$ $604 + 90 =$ </p>																							
Hundreds	Tens	Ones																																			
H	T	O																																			
<p>Add two numbers (no exchange)</p> <p>Mental strategies and introduction of formal written method.</p>	<p>... ones + ... ones = ... ones ... tens + ... tens = ... tens ... hundreds + ... hundreds = ... hundreds</p> <table border="1" data-bbox="683 1114 1104 1307"> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p></p> <table border="1" data-bbox="1339 1098 1753 1291"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <table border="1" data-bbox="1603 986 1977 1066"> <tr> <td colspan="2">?</td> </tr> <tr> <td>345</td> <td>432</td> </tr> </table> <table border="1" data-bbox="1765 1098 1977 1313"> <thead> <tr> <th></th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>+</td> <td>4</td> <td>3</td> <td>2</td> </tr> <tr> <td colspan="4"><hr/></td> </tr> </tbody> </table>								Hundreds	Tens	Ones							?		345	432		H	T	O		3	4	5	+	4	3	2	<hr/>			
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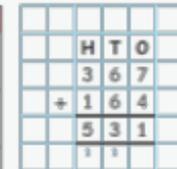
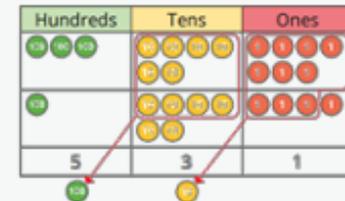
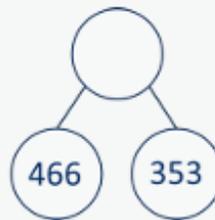
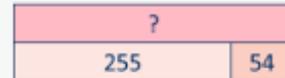
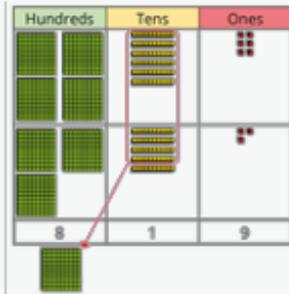
Progression of skills

Key representations

Add two numbers across a 10 or 100

Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.

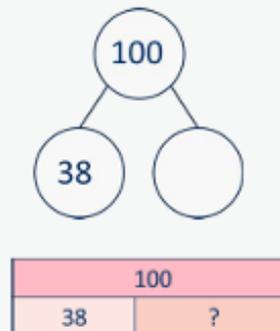
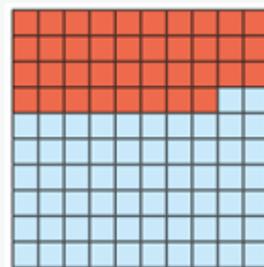
There are ... ones, so I do/do not need to make an exchange.
 There are ... tens, so I do/do not need to make an exchange.
 ... ones = ... ten and ... ones.
 ... tens = ... hundred and ... tens.



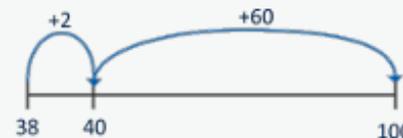
Complements to 100

Pairs of numbers which total 100

... plus ... is equal to 100



I add ... to get to the next 10, then ... to get to 100

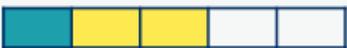
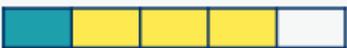
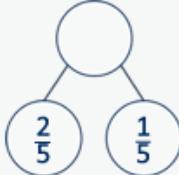
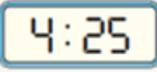
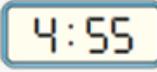
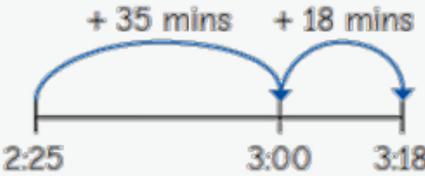


$$38 + 62 = 100$$

$$62 + 38 = 100$$

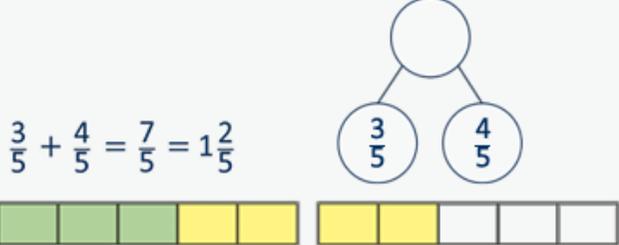
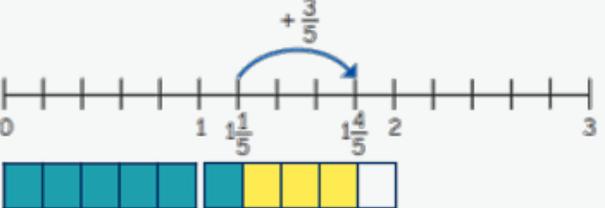
$$100 = 38 + 62$$

$$100 = 62 + 38$$

Progression of skills	Key representations
<p>Add fractions with the same denominator within 1 whole</p> <p>Make links with known facts.</p>	<p>When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  $\frac{1}{5} + \frac{1}{5}$ </div> <div style="text-align: center;">  $\frac{1}{5} + \frac{2}{5}$ </div> <div style="text-align: center;">  $\frac{1}{5} + \frac{3}{5}$ </div> </div> <div style="text-align: right; margin-top: 20px;">  </div> <div style="text-align: right; margin-top: 20px;">  </div>
<p>Calculate the duration of events</p> <p>Find durations of time between a given start and end point. Children will need to calculate complements to 60</p>	<p>From ... to ... o'clock is ... minutes. From ... o'clock to ... is ... minutes. The total time taken is ... minutes.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>start</p> </div> <div style="text-align: center;">  <p>finish</p> </div> <div style="text-align: center;">  <p>start</p> </div> <div style="text-align: center;">  <p>finish</p> </div> <div style="text-align: center;">  </div> </div>

Addition - Year 4

<p>Year 4</p>	<ul style="list-style-type: none"> • Add numbers with up to 4 digits using a formal written method. • Solve simple measure and money problems involving fractions and decimals to 2 decimal places. • Add fractions with the same denominator. 																																											
<p>Progression of skills</p>	<p>Key representations</p>																																											
<p>Add 1s, 10s and 100s to a 4-digit number</p> <p>Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.</p>	<p>The ones/tens/hundreds/thousands column will increase by ...</p> <table border="1" data-bbox="674 619 1122 802"> <thead> <tr> <th>Thousands</th> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td>1,000 1,000 1,000</td> <td>100 100 100 100</td> <td>10 30</td> <td>1 1 1 1 1</td> </tr> </tbody> </table> <p> $3,425 + 3 =$ $3,425 + 300 =$ $3,425 + 30 =$ $3,425 + 3,000 =$ </p>	Thousands	Hundreds	Tens	Ones	1,000 1,000 1,000	100 100 100 100	10 30	1 1 1 1 1	<p>What patterns do you notice?</p> <p> $2,350 + 3 =$ $2,350 + 30 =$ $2,350 + 300 =$ $2,350 + 3,000 =$ </p> <p> $6,040 + 200 =$ $2,211 + \square = 2,251$ $6,040 + 500 =$ $2,211 + \square = 2,215$ $6,040 + 900 =$ $2,211 + \square = 2,511$ </p>																																		
Thousands	Hundreds	Tens	Ones																																									
1,000 1,000 1,000	100 100 100 100	10 30	1 1 1 1 1																																									
<p>Add up to two 4-digit numbers</p> <p>Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<p>There are ... ones/tens/hundreds so I do/do not need to make an exchange.</p> <p>I can exchange 10 ... for 1 ...</p> <table border="1" data-bbox="1296 963 1599 1321"> <thead> <tr> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1,000 1,000 1,000 1,000</td> <td>100 100 100 100 100 100</td> <td>10 10 10 10 10 10</td> <td>1 1 1 1 1 1</td> </tr> <tr> <td>1,000</td> <td>100 100 100 100 100</td> <td>10</td> <td>1 1 1 1 1 1 1 1</td> </tr> </tbody> </table> <table border="1" data-bbox="1677 1031 1924 1241"> <tbody> <tr> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td>Th</td> <td>H</td> <td>T</td> <td>O</td> </tr> <tr> <td></td> <td>4</td> <td>6</td> <td>7</td> <td>3</td> </tr> <tr> <td>+</td> <td>1</td> <td>5</td> <td>1</td> <td>8</td> </tr> <tr> <td></td> <td>6</td> <td>1</td> <td>9</td> <td>1</td> </tr> <tr> <td></td> <td>1</td> <td>0</td> <td></td> <td></td> </tr> </tbody> </table>		Th	H	T	O	1,000 1,000 1,000 1,000	100 100 100 100 100 100	10 10 10 10 10 10	1 1 1 1 1 1	1,000	100 100 100 100 100	10	1 1 1 1 1 1 1 1							Th	H	T	O		4	6	7	3	+	1	5	1	8		6	1	9	1		1	0		
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Progression of skills	Key representations	
<p>Add decimal numbers in the context of money</p> <p>Emphasis on partitioning and use of number lines rather than formal written calculations.</p>	<p>... pence + ... pence = ... pence ... pounds + ... pounds = ... pounds</p>  <p>45p + 25p = 70p £2 + £3 = £5 £5 + 70p = £5.70</p>	<p>£3.25 can be partitioned into £3 + 20p + 5p</p> 
<p>Add fractions and mixed numbers with the same denominator beyond 1 whole</p>	<p>When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths</p>  	

Progression of skills	Key representations
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Add decimals with up to 2 decimal places

Progress from the same number of decimal places to a different number of decimal places, and from no exchange to exchange.

I do/do not need to make an exchange because ...
I can exchange 10 ... for 1 ...

Ones	Tenths	Hundredths
1 1 1	0.1 0.1 0.1	0.01 0.01 0.01
1	0.1	0.01 0.01
1 1 1	0.1 0.1	0.01

		4	4	5	
		+	3	2	1

O	Tth	Hth	Thth
1	0.1 0.1	0.01 0.01	0.001
1	0.1 0.1	0.01 0.01	0.01 0.01
1	0.1 0.1	0.01 0.01	0.01 0.01
1	0.1 0.1	0.01 0.01	0.01 0.01

		1	2	8	1
		+	2	5	4

Complements to 1

Pairs of numbers with up to 3 decimal places which total 1

Encourage children to make links with bonds to 10 and complements to 100 and 1,000

$0.3 + \square = 1$

1					
1					
1					
1					
1					
1					
1					
1					
1					
1					

$0.35 + \square = 1$

1					
1					
1					
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1					

1

0.4

○

1

○

0.44

1

○

0.444

$4 + 6 = 10$

$44 + 56 = 100$

$444 + 556 = 1,000$

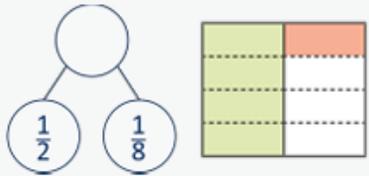
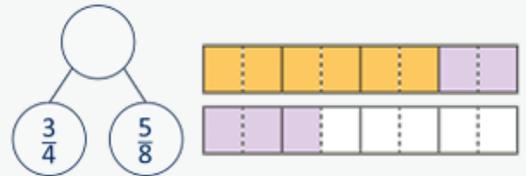
$0.4 + 0.6 = 1$

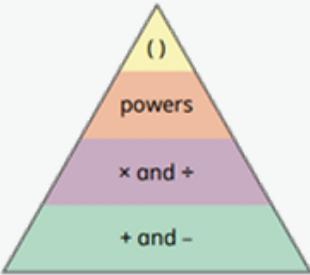
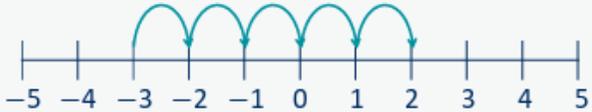
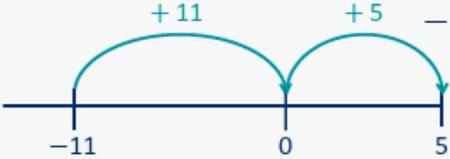
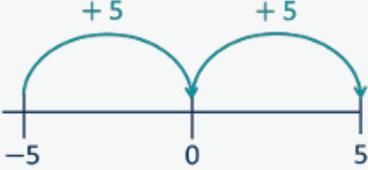
$0.44 + 0.56 = 1$

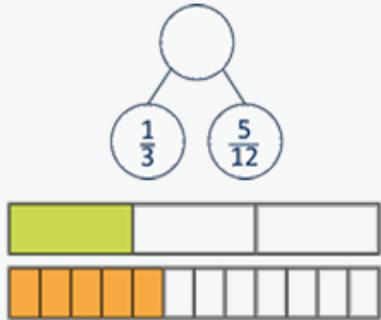
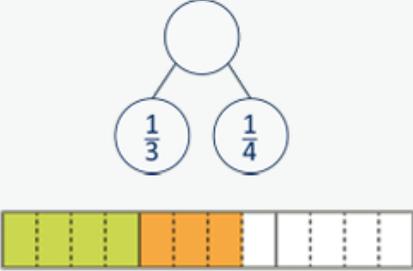
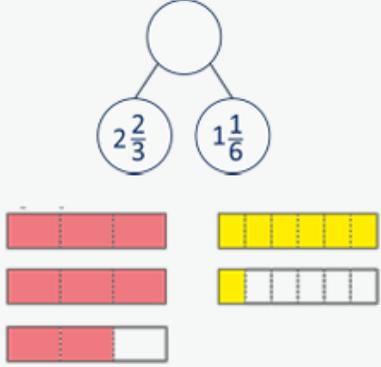
$0.444 + 0.556 = 1$

71	29
100	

0.71	0.29
1	

Progression of skills	Key representations
<p>Add fractions with denominators that are a multiple of one another</p> <p>Encourage children to convert fractions to the same denominator before adding.</p> <p>Progress from adding fractions within 1 whole to adding fractions beyond 1 whole.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  $\frac{1}{2} + \frac{1}{8} = \frac{4}{8} + \frac{1}{8} = \frac{5}{8}$ </div> <div style="text-align: center;">  $\frac{3}{4} + \frac{5}{8} = \frac{6}{8} + \frac{5}{8} = \frac{11}{8} = 1\frac{3}{8}$ </div> </div> <div style="display: flex; justify-content: space-around; align-items: flex-start; margin-top: 20px;"> <div style="text-align: center;">  $\frac{1}{4} + \frac{3}{8} = \frac{2}{8} + \frac{3}{8} = \frac{5}{8}$ </div> </div>

Progression of skills	Key representations	
<p>Order of operations</p> <p>Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets are shown and the operations have the same priority, work left to right.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p> 	 <p>$(3 + 4) \times 2 = 14$</p>  <p>$3 + 4 \times 2 = 11$</p>  <p>$3 \times 4 + 2 = 14$</p>
<p>Negative numbers</p> <p>Children add to negative numbers and carry out calculations which cross 0</p>	<p>... plus ... is equal to ...</p> <p>$-3 + 5 = 2$</p>  <p>$-11 + 16 = 5$</p> 	 <p>The difference between -5 and -1 is 4</p>  <p>The difference between -5 and 5 is 10</p>

Progression of skills	Key representations		
<p>Add fractions</p> <p>Convert fractions to the same denominator before adding. Progress from fractions where one denominator is a multiple of the other, to any fractions and then to mixed numbers.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by ...</p> 	<p>The lowest common multiple of ... and ... is ...</p>  $\frac{1}{3} + \frac{1}{4} = \frac{4}{12} + \frac{3}{12} = \frac{7}{12}$	<p>...is made up of ... wholes and ...</p> 

Subtraction - Nursery

<p>Nursery</p>	<ul style="list-style-type: none"> • Begin to have an understanding of numbers to 5 • We recommend focusing on noticing and representing small quantities, perceptual subitising and counting. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Subitise to 3</p> <p>Instantly see how many.</p>	<p>How many do you see?</p> 	
<p>Count how many</p> <p>Begin to count objects using 1-1 correspondence.</p>	<p>How many are there?</p> <p>1 2 3 4 5</p> 	<p>Count out ... from a larger group.</p> <p>E.g. Collect a cup for everyone at the table.</p> 
<p>Make numbers to 5</p> <p>Start by showing 1, 2 and 3 using fingers.</p>	<p>Show me...</p> 	<p>Begin to link numerals to quantities.</p> 
<p>Take 1 away</p> <p>Through stories, songs and rhymes.</p>	<p>How many do we have now?</p> 	

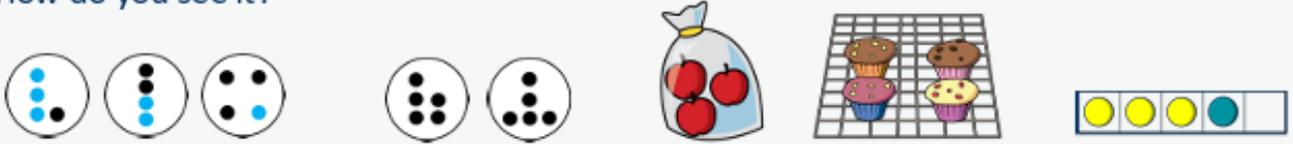
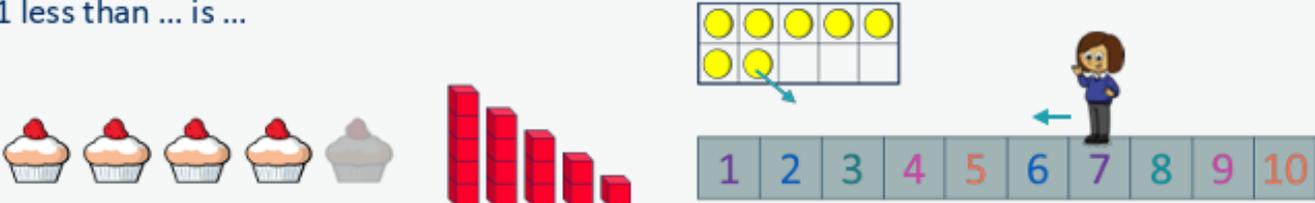
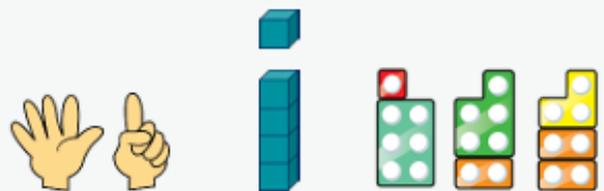
Progression of Skills - Subtraction

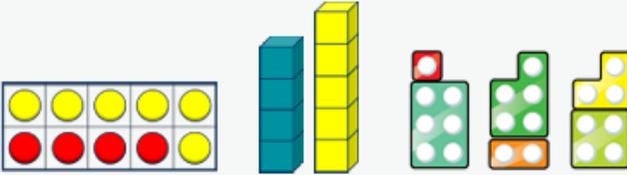
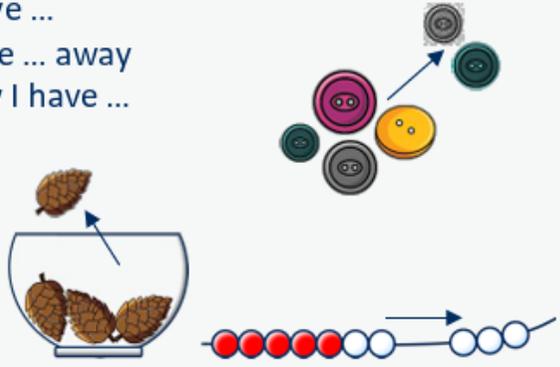
Year group	Skill
Nursery	<ul style="list-style-type: none">• Subitise to 3• Count how many• Make numbers to 5• Take 1 away (through songs and rhymes)
Reception	<ul style="list-style-type: none">• Conceptually subitise to 5• 1 less• Notice the composition of numbers within 10• Partition• Take away
Year 1	<ul style="list-style-type: none">• Find a part• Take away• Bonds within 10• Related facts within 20• Missing numbers

Year group	Skill
Year 2	<ul style="list-style-type: none">• Subtract 1s from any number (related facts)• Subtract across a 10• Subtract multiples of 10• Subtract 10s from any number• Subtract two 2-digit numbers (not across a ten)• Subtract two 2-digit numbers (across a ten)• Missing numbers
Year 3	<ul style="list-style-type: none">• Subtract 1s, 10s and 100s from a 3-digit number• Subtract two numbers (no exchange)• Subtract two numbers across a 10 or 100• Complements to 100• Subtract fractions with the same denominator within 1 whole

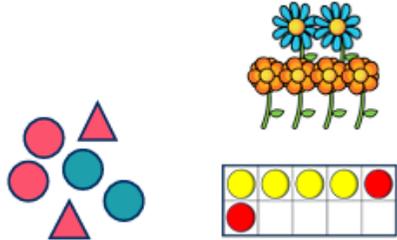
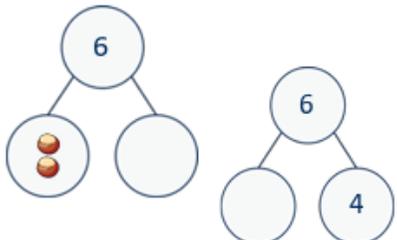
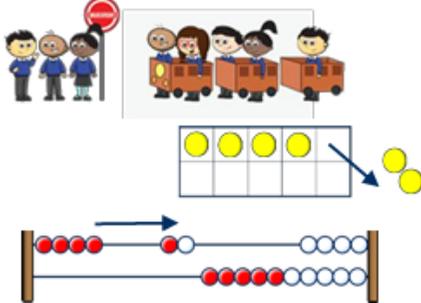
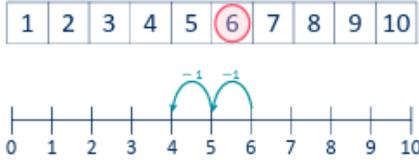
Year group	Skill
Year 4	<ul style="list-style-type: none">• Subtract 1s, 10s, 100s and 1,000s from a 4-digit number• Subtract up to two 4-digit numbers• Subtract decimal numbers in the context of money• Subtract fractions and mixed numbers with the same denominator
Year 5	<ul style="list-style-type: none">• Subtract whole numbers with more than 4 digits• Subtract using mental strategies• Subtract decimals with up to 2 decimal places• Complements to 1• Subtract fractions with denominators that are a multiple of one another
Year 6	<ul style="list-style-type: none">• Subtract integers up to 10 million• Subtract decimals with up to 3 decimal places• Order of operations• Negative numbers• Subtract fractions

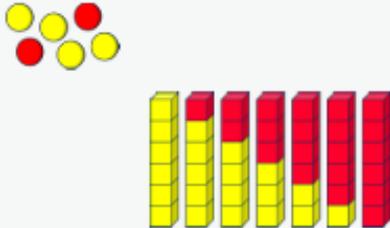
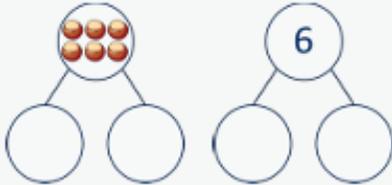
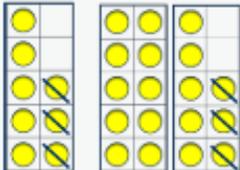
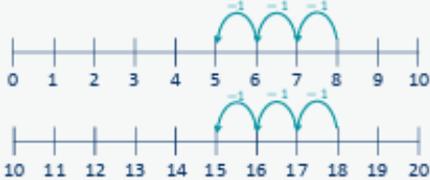
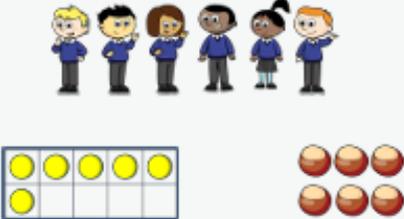
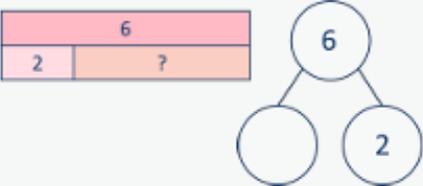
Subtraction - Reception

<p>Reception</p>	<ul style="list-style-type: none"> • Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (and some subtraction facts) and some number bonds to 10, including double facts. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Conceptually subitise to 5</p> <p>Notice the parts that make up the whole.</p>	<p>What do you see? How do you see it?</p> 	
<p>1 less</p> <p>Continue to link to stories, songs and rhymes.</p>	<p>1 less than ... is ...</p> 	
<p>Notice the composition of numbers within 10</p> <p>Link to stories, songs and rhymes.</p>	<p>How many...? How many...? How many altogether?</p> 	<p>How many ways can you make...?</p> 

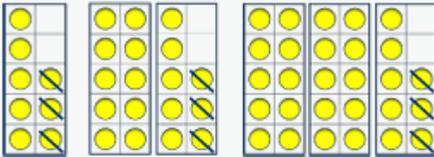
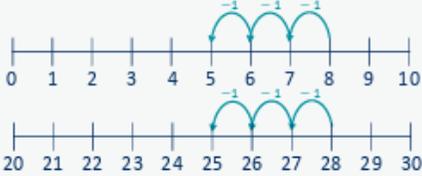
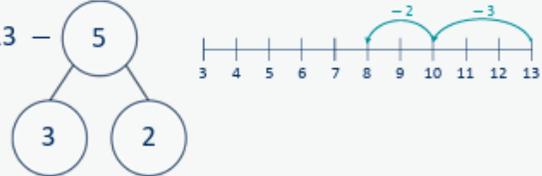
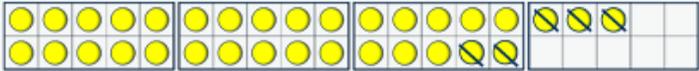
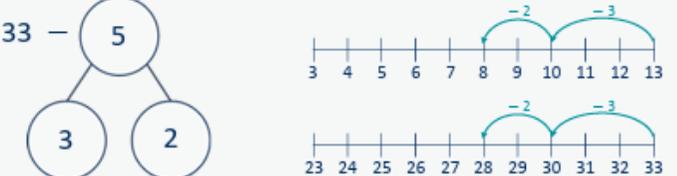
Progression of skills	Key representations	
<p>Partition</p> <p>Using objects, explore different ways to partition a number into 2 or more parts.</p>	<p>There are ... altogether. I can see ... here and ... there.</p> 	<p>... and ... make ...</p> 
<p>Take away</p> <p>A quantity is reduced.</p>	<p>First... Then... Now...</p> 	<p>I have ... I take ... away Now I have ...</p> 

Subtraction - Year 1

<p>Year 1</p>	<ul style="list-style-type: none"> • Read, write and interpret mathematical statements involving subtraction (–) and equals (=) signs. • Represent and use number bonds and related subtraction facts within 20 • Subtract one-digit and two-digit numbers to 20, including zero. • Solve one-step problems that involve subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$ 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Find a part</p> <p>Link to number bonds and known facts. E.g. $2 + 4 = 6$ so if 6 is the whole and 4 is a part, the other part must be 2</p>	<p>There are ... in total. ... are ... How many are not ...?</p> 	<p>... is the whole. ... is a part. ... is a part.</p> 	<p>... subtract ... is equal to is equal to ... – ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
<p>Take away</p> <p>A quantity is decreased.</p>	<p>First... Then... Now...</p> 	<p>I start at ... I jump back ... I land on ...</p> 	<p>... minus ... is equal to is equal to ... – ...</p> $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$

Progression of skills	Key representations		
<p>Bonds within 10</p> <p>Focus on subtraction facts.</p> <p>Encourage children to notice patterns.</p>	<p>... is made of ... and and ... make ...</p> 	<p>... can be partitioned into ... and ...</p> 	<p>... minus ... is equal to ...</p> $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$
<p>Related facts within 20</p> <p>Make links to known facts.</p>	<p>I know that ... minus ... = ... so ... minus ... = ...</p> 	<p>... less than ... is ... so ... less than ... is ...</p> 	<p>What patterns do you notice?</p> $8 - 3 = 5$ $18 - 3 = 15$ $5 = 8 - 3$ $15 = 18 - 3$
<p>Missing numbers</p> <p>Make links to known facts.</p>	<p>How many do you need to subtract to make ...?</p> 	<p>If ... is the whole and ... is a part, the other part must be...</p> 	<p>... minus ... is equal to ...</p> $6 - \square = 2$ $2 = 6 - \square$ 

Subtraction - Year 2

	<ul style="list-style-type: none"> Recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100 Subtract numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> a two-digit number and 1s a two-digit number and 10s 2 two-digit numbers Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Subtract ones from any number (related facts)</p> <p>Make links to known facts.</p>	<p>I know that ... minus ... = ... so ... minus ... = ...</p> 	<p>... less than ... is ... so ... less than ... is ...</p> 	<p>What do you notice? Can you continue the pattern?</p> $8 - 3 = 5$ $18 - 3 = 15$ $28 - 3 = 25...$
<p>Subtract across a 10</p> <p>Partition the number being subtracted to bridge through a ten.</p>	<p>... can be partitioned into ... and ...</p>  <p>13 - 5</p> 		<p>Make links with related facts.</p>  <p>33 - 5</p> 

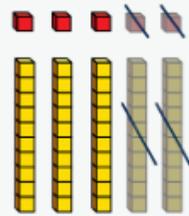
Progression of skills

Key representations

Subtract multiples of 10

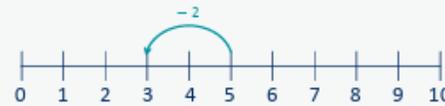
Make links to known facts within ten.

... ones – ... ones = ... ones
so ... tens – ... tens = ... tens



$5 - 2 = 3$
 $50 - 20 = 30$

What is the same?
What is different?



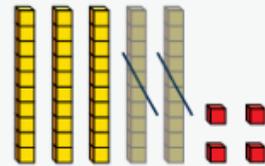
5	
2	?

50	
20	?

Subtract 10s from any number

Make links to known facts.

... tens – ... tens = ... tens
... tens and ... ones = ...

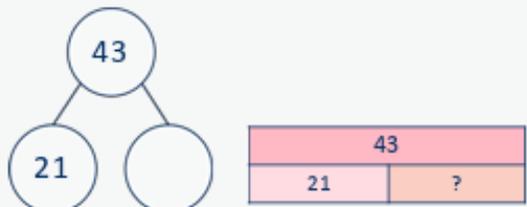
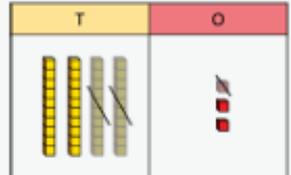
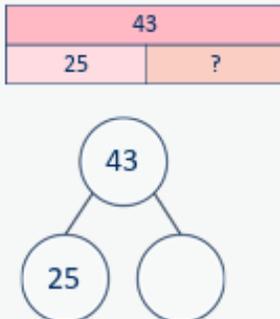
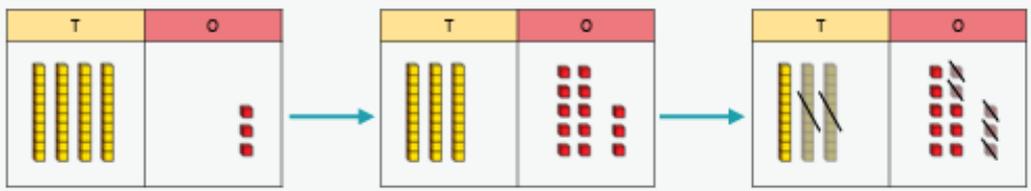
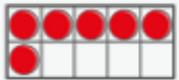
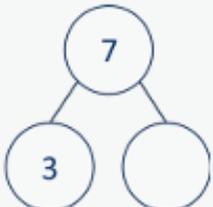
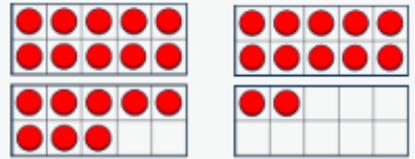


To subtract ... I need to subtract 10 ... times.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60

I know that ... minus ... = ...
so ... minus ... = ...

$50 - 20 = 30$
 $54 - 20 = 34$

Progression of skills	Key representations		
<p>Subtract two 2-digit numbers (not across a ten)</p>	<p>... ones - ... ones = ... ones ... tens - ... tens = ... tens</p>   <p>3 ones - 1 one = 2 ones 4 tens - 2 tens = 2 tens 2 tens and 2 ones = 22</p>		
<p>Subtract two 2-digit numbers (across a ten)</p> <p>Begin to exchange 1 ten for 10 ones.</p>	<p>I need to make an exchange because I do not have enough ones to subtract ... ones.</p>   <p>3 ones - 5 ones (I need to exchange 1 ten for 10 ones)</p> <p>13 ones - 5 ones = 8 ones 3 tens - 2 tens = 1 ten 1 ten and 8 ones = 18</p>		
<p>Missing numbers</p> <p>Solve missing number problems and use the inverse to check.</p>	<p>How many do you need to subtract to make ...?</p>  <p>$10 - \square = 6$ $6 + \square = 10$</p>	<p>If ... is a whole and ... is a part, then ... is the other part.</p> <p>$7 - 3 = \square$ $\square + 3 = 7$</p> 	<p>... can be partitioned into ... and ...</p> <p>$18 - \square = 12 + 2$</p> 

Subtraction - Year 3

Year 3

- Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds.
- Subtract numbers with up to three digits, using formal written methods.
- Subtract fractions with the same denominator within 1 whole.

Progression of skills **Key representations**

Subtract 1s, 10s and 100s from a 3-digit number

Emphasis on mental strategies including number bonds and related facts.
 Prompt children to notice which digit changes.

The ones/tens/hundreds column will decrease by ...

Hundreds	Tens	Ones

H	T	O

$444 - 2 =$ $777 - 4 =$
 $444 - 20 =$ $777 - 40 =$
 $444 - 200 =$ $777 - 400 =$

What patterns do you notice?

$235 - 3 =$
 $235 - 30 =$
 $235 - 300 =$

$118 -$	<input type="text"/>	$= 111$
$624 - 20 =$	<input type="text"/>	$= 111$
$654 - 50 =$	<input type="text"/>	$= 111$
$694 - 90 =$	<input type="text"/>	$= 111$

Subtract two numbers (no exchange)

Mental strategies and introduction of formal written method.

... ones – ... ones = ... ones
 ... tens – ... tens = ... tens
 ... hundreds – ... hundreds = ... hundreds

769	
147	?

Hundreds	Tens	Ones

H	T	O

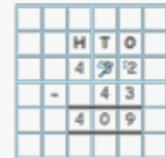
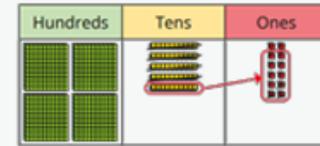
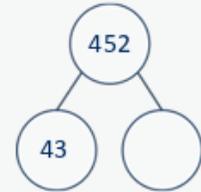
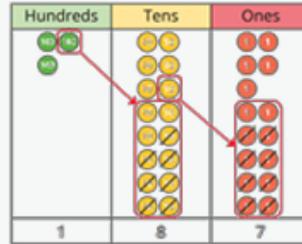
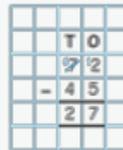
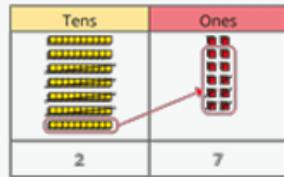
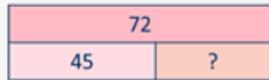
H	T	O
7	6	9
-	1	4
<hr/>		

Progression of skills	Key representations
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Subtract two numbers across a 10 or 100

Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.

I need to subtract ... ones. I do/do not need to make an exchange.
 I need to subtract ... tens. I do/do not need to make an exchange.
 I can exchange 1 ... for 10 ...

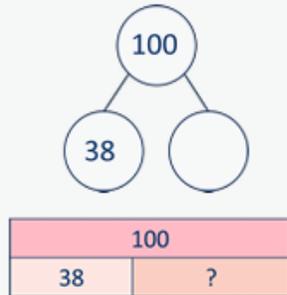
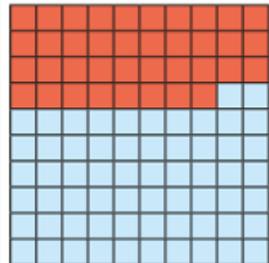


Complements to 100

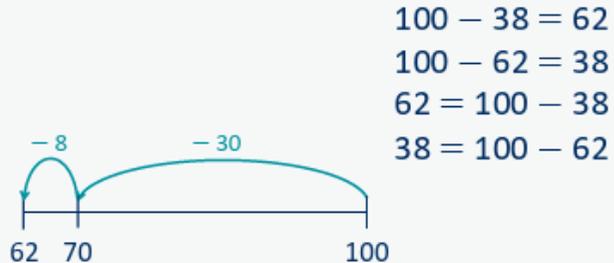
Focus on subtraction facts.

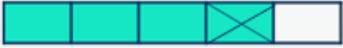
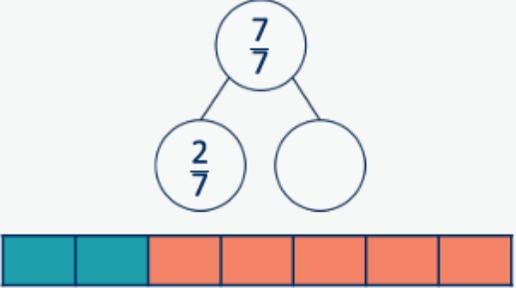
Encourage children to notice patterns.

100 minus ... is equal to ...



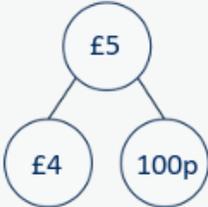
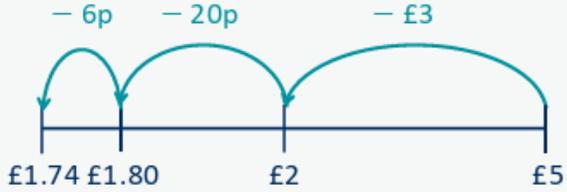
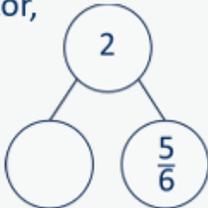
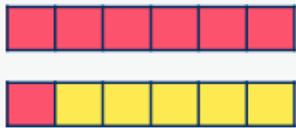
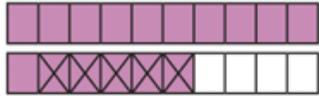
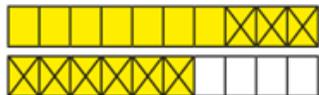
I subtract ... tens, then I subtract ... ones.



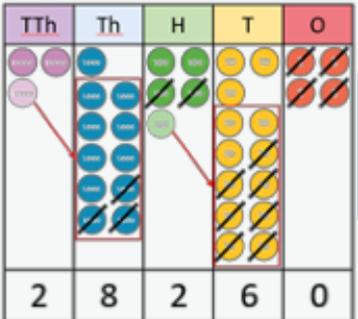
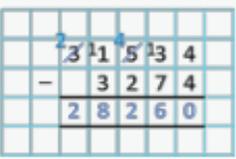
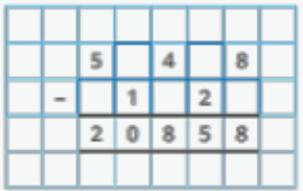
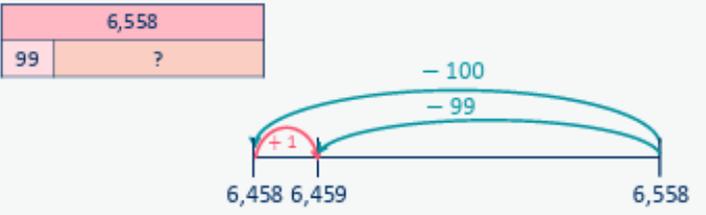
Progression of skills	Key representations
<p>Subtract fractions with the same denominator within 1 whole</p> <p>Make links with known facts.</p>	<p>When subtracting fractions with the same denominator, I only subtract the numerator. ... fifths – ... fifths = ... fifths</p> <div style="display: flex; align-items: center; margin-bottom: 10px;">  <div style="margin-left: 10px;">$\frac{4}{5} - \frac{1}{5}$</div> </div> <div style="display: flex; align-items: center; margin-bottom: 10px;">  <div style="margin-left: 10px;">$\frac{3}{5} - \frac{1}{5}$</div> </div> <div style="display: flex; align-items: center;">  <div style="margin-left: 10px;">$\frac{2}{5} - \frac{1}{5}$</div> </div> <div style="text-align: right; margin-top: 20px;">  </div>

Subtraction - Year 4

<p>Year 4</p>	<ul style="list-style-type: none"> Subtract numbers with up to 4 digits using a formal written method. Solve simple measure and money problems involving fractions and decimals to 2 decimal places. Subtract fractions with the same denominator. 																																																																	
<p>Progression of skills</p>	<p>Key representations</p>																																																																	
<p>Subtract 1s, 10s, 100s and 1,000s from a 4-digit number</p> <p>Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.</p>	<p>The ones/tens/hundreds/thousands column will decrease by ...</p> <table border="1" data-bbox="674 571 1122 756"> <thead> <tr> <th>Thousands</th> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td>1,000 1,000 1,000</td> <td>100 100 100 100</td> <td>10 10</td> <td>1 1 1 1 1</td> </tr> </tbody> </table> <p> $3,425 - 2 =$ $3,425 - 200 =$ $3,425 - 20 =$ $3,425 - 2,000 =$ </p>	Thousands	Hundreds	Tens	Ones	1,000 1,000 1,000	100 100 100 100	10 10	1 1 1 1 1	<p>What patterns do you notice?</p> <p> $4,356 - 3 =$ $4,356 - 30 =$ $4,356 - 300 =$ $4,356 - 3,000 =$ </p> <p> $4,433 - \square = 4,430$ $4,433 - \square = 4,033$ $4,433 - \square = 4,403$ </p>																																																								
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<p>Subtract up to two 4-digit numbers</p> <p>Formal written method with up to 3 exchanges. Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<p>I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange.</p> <p>I can exchange 1... for 10...</p> <table border="1" data-bbox="1153 997 1637 1316"> <thead> <tr> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>1,000 1,000</td> <td>100 100</td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td>100 100</td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> <tr> <td></td> <td></td> <td>10 10 10</td> <td>1 1 1</td> </tr> </tbody> </table> <table border="1" data-bbox="1668 1034 1955 1281"> <thead> <tr> <th></th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td>3</td> <td>2</td> <td>4</td> <td>8</td> </tr> <tr> <td>-</td> <td>2</td> <td>1</td> <td>4</td> <td>8</td> </tr> <tr> <td></td> <td>1</td> <td>0</td> <td>5</td> <td>8</td> </tr> </tbody> </table>		Th	H	T	O	1,000 1,000	100 100	10 10 10	1 1 1		100 100	10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1			10 10 10	1 1 1		Th	H	T	O		3	2	4	8	-	2	1	4	8		1	0	5	8
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Progression of skills	Key representations	
<p>Subtract decimal numbers in the context of money</p> <p>Emphasis here is on partitioning and use of number lines rather than formal written calculations.</p>	<p>I can partition £... into £... and 100p</p> <p>£... - £... = £...</p> <p>100p - ...p = ...p</p> <p>£5 - £3.26 £4 - £3 = £1 100p - 26p = 74p £5 - £3.26 = £1.74</p> 	<p>£3.26 can be partitioned into £3 + 20p + 6p</p> 
<p>Subtract fractions and mixed numbers with the same denominator</p> <p>Include subtracting fractions from wholes.</p>	<p>When subtracting fractions with the same denominator, I only subtract the numerator.</p> <p>... tenths - ... tenths = ... tenths</p>    $\frac{16}{10} - \frac{5}{10}$  $\frac{16}{10} - \frac{9}{10}$  	

Subtraction - Year 5

<p>Year 5</p>	<ul style="list-style-type: none"> Subtract whole numbers with more than 4 digits. Subtract numbers mentally with increasingly large numbers. Subtract decimals, including a mix of whole numbers and decimals, decimals with different numbers of decimal places, and complements of 1 Subtract fractions with the same denominator, and denominators that are multiples of the same number. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Subtract whole numbers with more than 4 digits</p> <p>Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<p>I can exchange 1 ... for 10 ...</p>   	
<p>Subtract using mental strategies</p> <p>Subtract 1s, 10s, 100s etc from any number. Use number bonds and related facts.</p>	 <p> $48,650 - 300 =$ $48,650 - 30,000 =$ $48,650 - 30 =$ </p>	<p>To subtract ..., I can subtract ... then add ...</p> 

Progression of skills	Key representations
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Subtract decimals with up to 2 decimal places

Progress from the same number of decimal places to a different number of decimal places and from no exchange to exchange.

The key representations include:

- A place value chart with columns for Ones, Tenths, and Hundredths. The Ones column has a 1 and a 0. The Tenths column has two 0.1s. The Hundredths column has four 0.01s.
- A grid showing the subtraction of 3.12 from 24.4. The grid is divided into three columns: Ones, Tenths, and Hundredths. The top row shows 2, 4, and 4. The second row shows a minus sign, 1, 1, and 2. The bottom row shows 1, 2, and 5.
- A number bond for 24.4 minus 3.12. The top circle is 24.4, and the bottom circles are 3.12 and a question mark.
- A grid showing the subtraction of 3.12 from 24.4. The grid is divided into three columns: Ones, Tenths, and Hundredths. The top row shows 2, 4, and 4. The second row shows a minus sign, 3, 1, and 2. The bottom row shows a horizontal line and a question mark.

Complements to 1

Encourage children to make links with bonds to 10 and complements to 100 and 1,000 when finding a missing part or subtracting from 1

The key representations include:

- Equations: $0.3 + \square = 1$ and $0.35 + \square = 1$
- Grids showing the complements of 0.3 and 0.35 to 1. The 0.3 grid has 3 columns shaded green. The 0.35 grid has 3 columns and 5 rows shaded blue.
- Number bonds for 1 minus 0.4, 1 minus 0.44, and 1 minus 0.444. The top circle is 1, and the bottom circles are 0.4, 0.44, and 0.444 respectively.
- Subtraction equations:
 - $10 - 4 = 6$
 - $100 - 44 = 56$
 - $1,000 - 444 = 556$
 - $1 - 0.4 = 0.6$
 - $1 - 0.44 = 0.56$
 - $1 - 0.444 = 0.556$

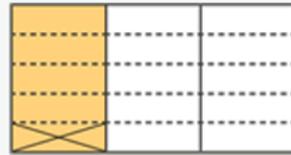
Progression of skills

Subtract fractions with denominators that are a multiple of one another

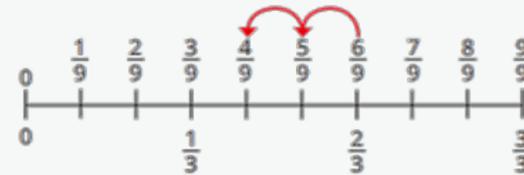
Convert fractions to the same denominator before subtracting. Progress from subtracting fractions within 1 whole to subtracting from a mixed number.

Key representations

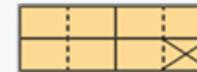
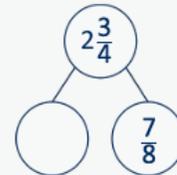
The denominator has been multiplied by ..., so the numerator needs to be multiplied by... for the fractions to be equivalent.



$$\frac{1}{3} - \frac{1}{15} = \frac{5}{15} - \frac{1}{15} = \frac{4}{15}$$

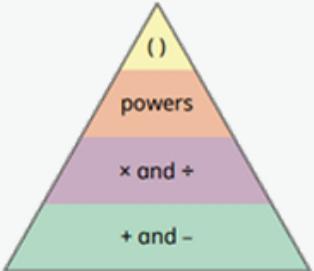
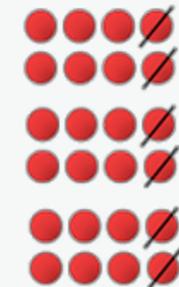
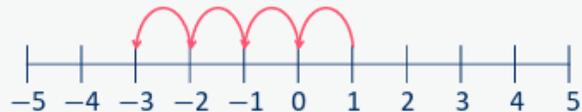
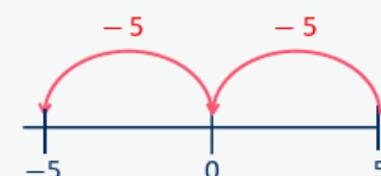


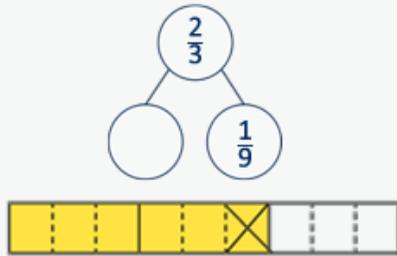
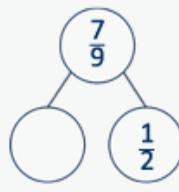
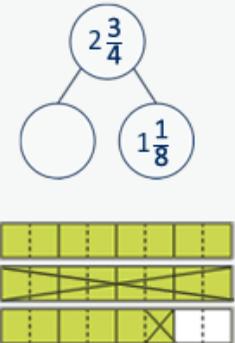
$$\frac{2}{3} - \frac{2}{9} = \frac{6}{9} - \frac{2}{9} = \frac{4}{9}$$



Subtraction - Year 6

<p>Year 6</p>	<ul style="list-style-type: none"> Subtract larger numbers, using the formal written methods of columnar subtraction. Use their knowledge of the order of operations to carry out calculations involving the 4 operations. Calculate intervals across zero. Subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions. 																																																																						
<p>Progression of skills</p>	<p>Key representations</p>																																																																						
<p>Subtract integers up to 10 million</p> <p>Encourage children to estimate and use inverse operations to check answers to calculations.</p>	<table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td>2</td><td>¹4</td><td>5</td><td>¹2</td><td>2</td><td>1</td><td></td></tr> <tr><td>-</td><td>1</td><td>8</td><td>4</td><td>3</td><td>2</td><td>1</td><td></td></tr> <tr><td></td><td>1</td><td>6</td><td>1</td><td>9</td><td>0</td><td>0</td><td></td></tr> </table> <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td colspan="3" style="background-color: #f8d7da;">4,604</td></tr> <tr><td style="background-color: #fff3cd;">2,354</td><td style="background-color: #fff3cd;">750</td><td style="background-color: #fff3cd;">?</td></tr> </table> <table border="1" style="display: inline-table;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td>8</td><td></td><td>4</td><td>8</td><td>5</td><td></td><td></td></tr> <tr><td>-</td><td>3</td><td>6</td><td></td><td></td><td></td><td>4</td><td></td></tr> <tr><td></td><td>5</td><td>5</td><td>5</td><td>5</td><td>5</td><td></td><td></td></tr> </table>										2	¹ 4	5	¹ 2	2	1		-	1	8	4	3	2	1			1	6	1	9	0	0		4,604			2,354	750	?										8		4	8	5			-	3	6				4			5	5	5	5	5		
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Progression of skills	Key representations	
<p>Order of operations</p> <p>Children learn the order of priority for operations in a calculation. Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ... , so the first part of the calculation I need to do is ...</p> <div style="display: flex; align-items: center; justify-content: space-around;"> <div data-bbox="750 367 1064 638" style="text-align: center;">  <p>() powers × and ÷ + and -</p> </div> <div style="text-align: center;">  <p>$8 - 2 \times 3 = 2$</p> </div> <div style="text-align: center;">  <p>$(8 - 2) \times 3 = 18$</p> </div> <div style="text-align: center;">  <p>$8 - 2^2 = 4$</p> </div> </div>	
<p>Negative numbers</p> <p>Children subtract from positive and negative numbers and calculate intervals across 0</p>	<p>... minus ... is equal to ...</p> <div style="display: flex; flex-direction: column; align-items: center;"> <div style="display: flex; align-items: center; margin-bottom: 20px;">  <div style="margin-left: 20px;">$-1 - 4 = -5$</div> </div> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;">$1 - 4 = -3$</div> </div> </div> <div style="display: flex; align-items: center; justify-content: space-around; margin-top: 20px;"> <div style="text-align: center;">  <p>The difference between -5 and -1 is 4</p> </div> <div style="text-align: center;">  <p>The difference between 5 and -5 is 10</p> </div> </div>	

Progression of skills	Key representations		
<p>Subtract fractions</p> <p>Convert fractions to the same denominator before subtracting. Progress from fractions where one denominator is a multiple of the other, to any fractions and then subtracting from a mixed number.</p>	<p>The denominator has been multiplied by ..., so the numerator needs to be multiplied by...</p>  $\frac{2}{3} - \frac{1}{9} = \frac{6}{9} - \frac{1}{9} = \frac{5}{9}$	<p>The lowest common multiple of ... and ... is ...</p>  $\frac{7}{9} - \frac{1}{2} = \frac{14}{18} - \frac{9}{18} = \frac{5}{18}$	<p>... is made up of ... wholes and ...</p>  $2\frac{3}{4} - 1\frac{1}{8} = 1\frac{5}{8}$

Progression of Skills - Multiplication

Year group	Skill
Nursery	<ul style="list-style-type: none">• Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)
Reception	<ul style="list-style-type: none">• Double to 10• Make equal groups
Year 1	<ul style="list-style-type: none">• Count in 2s, 5s and 10s• Add equal groups• Make arrays• Make doubles

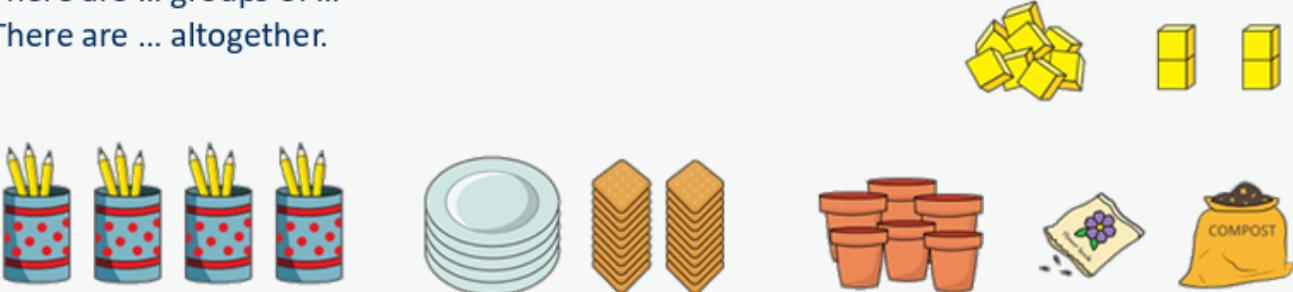
Year group	Skill
Year 2	<ul style="list-style-type: none">• Link repeated addition and multiplication• Use arrays• Double• The 2 times-table• The 10 times-table• The 5 times-table• Missing numbers
Year 3	<ul style="list-style-type: none">• The 3 times-table• The 4 times-table• The 8 times-table• Related facts• Multiply a 2-digit number by a 1-digit number - no exchange• Multiply a 2-digit number by a 1-digit number - with exchange• Scaling• Correspondence problems

Year group	Skill
Year 4	<ul style="list-style-type: none">• Times-table facts to 12×12• Multiply by 1 and 0• Multiply 3 numbers• Factor pairs• Multiply by 10 and 100• Related facts• Mental strategies• Multiply a 2 or 3-digit number by a 1-digit number• Scaling• Correspondence problems

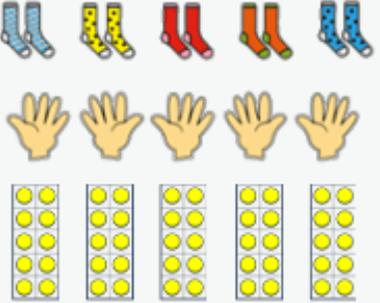
Year group	Skill
Year 5	<ul style="list-style-type: none"><li data-bbox="618 233 1032 272">• Multiples and factors<li data-bbox="618 312 1122 352">• Square and cube numbers<li data-bbox="618 392 1541 432">• Multiply numbers up to 4 digits by a 1-digit number<li data-bbox="618 472 1541 512">• Multiply numbers up to 4 digits by a 2-digit number<li data-bbox="618 552 1178 592">• Multiply by 10, 100 and 1,000<li data-bbox="618 632 969 671">• Mental strategies<li data-bbox="618 711 1308 751">• Multiply fractions by a whole number<li data-bbox="618 791 1420 831">• Multiply mixed numbers by a whole number<li data-bbox="618 871 927 911">• Find the whole

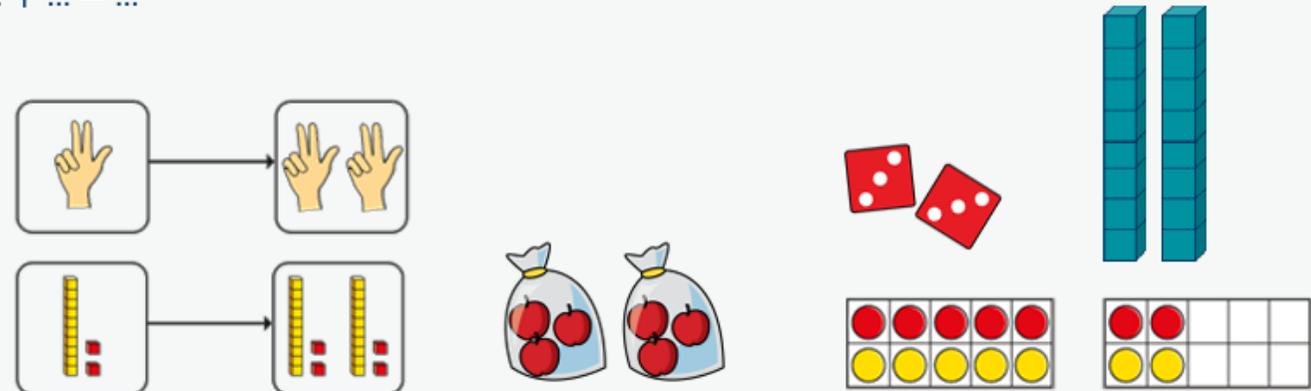
Year group	Skill
Year 6	<ul style="list-style-type: none"><li data-bbox="618 240 1541 277">• Multiply numbers up to 4 digits by a 2-digit number<li data-bbox="618 323 1178 360">• Multiply by 10, 100 and 1,000<li data-bbox="618 406 1010 443">• Order of operations<li data-bbox="618 489 1167 526">• Multiply decimals by integers<li data-bbox="618 572 1178 609">• Multiply fractions by fractions<li data-bbox="618 655 927 692">• Find the whole<li data-bbox="618 738 1128 775">• Calculations involving ratio

Multiplication - Reception

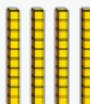
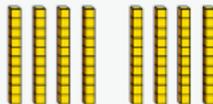
<p>Reception</p>	<ul style="list-style-type: none"> • Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. • Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.
<p>Progression of skills</p>	<p>Key representations</p>
<p>Double to 10</p> <p>Prompt children to notice that double means twice as many and to notice that there are two equal groups.</p>	<p>Double ... is is double ...</p> 
<p>Make equal groups</p> <p>Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.</p>	<p>There are ... groups of ... There are ... altogether.</p> 

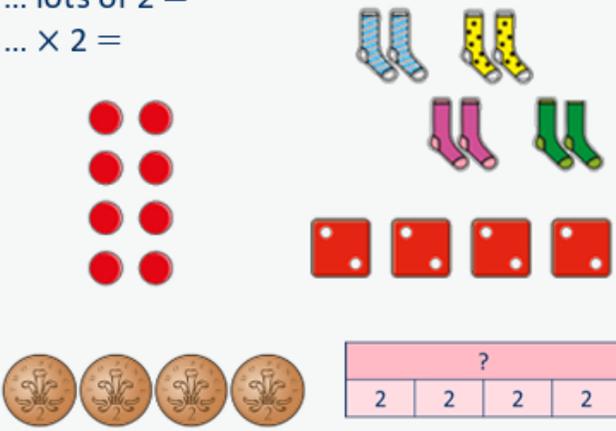
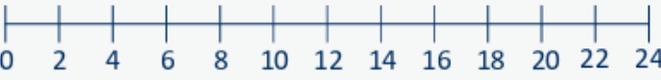
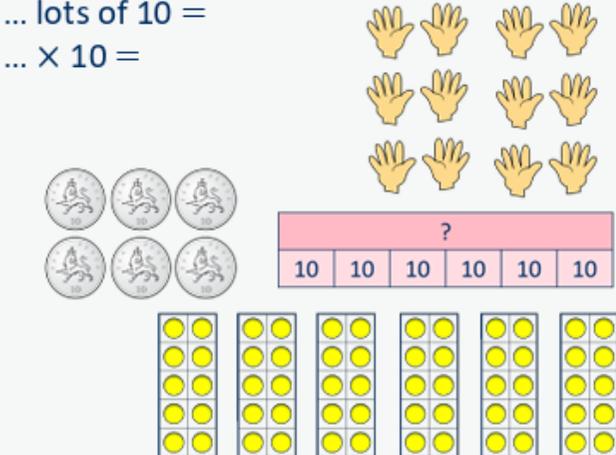
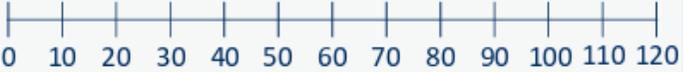
Multiplication - Year 1

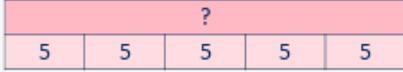
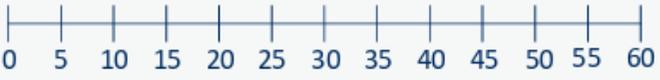
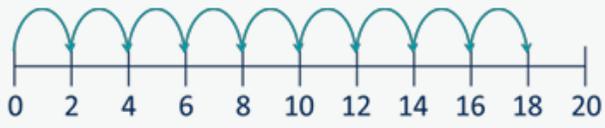
Year 1	<ul style="list-style-type: none"> Count in multiples of twos, fives and tens. Solve one-step problems involving multiplication, using concrete objects, pictorial representations and arrays with the support of the teacher. 																																																												
Progression of skills	Key representations																																																												
<p>Count in 2s, 5s and 10s</p> <p>Begin by counting objects that naturally come in 2s, 5s and 10s, for example pairs of socks or fingers.</p>	<p>There are ... equal groups of ... There are ... altogether.</p> 	<p>Continue to colour in ...s What do you notice?</p> <table border="1" data-bbox="1187 630 1556 813"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	<p>Complete the number track/number line by counting in ...s.</p> <table border="1" data-bbox="1590 646 2004 694"> <tr> <td>5</td> <td>10</td> <td>15</td> <td>20</td> <td></td> <td></td> <td></td> <td></td> </tr> </table> 	5	10	15	20				
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<p>Add equal groups (repeated addition)</p> <p>Children should be able to write a repeated addition to represent equal groups and to draw pictures or use objects to represent a repeated addition.</p>	<p>There are ... groups of ... There are ... altogether.</p>  $10 + 10 + 10 = 30$  $5 + 5 + 5 + 5 = 20$		<p>What is the same? What is different?</p> $2 + 2 + 2 =$ $5 + 5 + 5 =$ $10 + 10 + 10 =$ <p>Use objects or a drawing to represent the equal groups and find how many in total.</p>																																																										

Progression of skills	Key representations
<p>Make arrays</p> <p>Children use their knowledge of adding equal groups to arrange objects in columns and rows.</p>	<p>There are ... rows of ... There are ... altogether. There are ... columns of ... There are ... altogether.</p> 
<p>Make doubles</p> <p>Children understand that doubles are two equal groups. Children may begin to explore doubles beyond 20 using base 10</p>	<p>Double ... is ... $\dots + \dots = \dots$</p> 

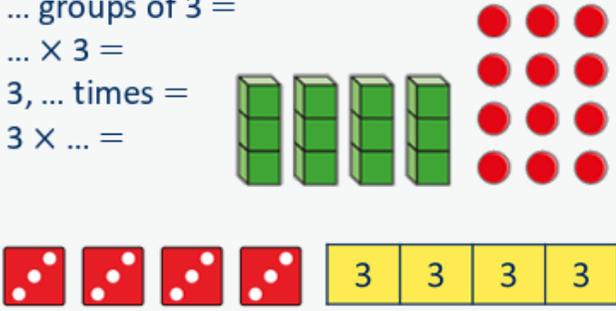
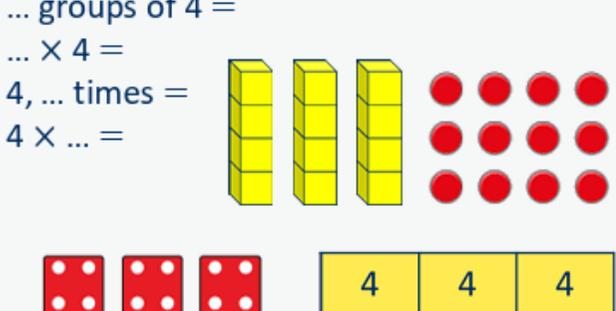
Multiplication - Year 2

<p>Year 2</p>	<ul style="list-style-type: none"> Recall and use multiplication facts for the 2, 5 and 10 multiplication tables. Calculate mathematical statements for multiplication within the multiplication tables and write them using the multiplication (\times) and equals ($=$) signs. Show that multiplication of two numbers can be done in any order (commutative). 													
<p>Progression of skills</p>	<p>Key representations</p>													
<p>Link repeated addition and multiplication</p> <p>Encourage children to make the link between repeated addition and multiplication.</p>	<p>There are ... equal groups with ... in each group. There are ... altogether.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse;"> <tr><td colspan="2" style="text-align: center;">6</td></tr> <tr><td style="text-align: center;">3</td><td style="text-align: center;">3</td></tr> </table> </div> <div style="text-align: left;"> <p>$3 + 3 = 6$ $2 \times 3 = 6$</p> </div> </div> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse;"> <tr><td colspan="4" style="text-align: center;">20</td></tr> <tr><td style="text-align: center;">5</td><td style="text-align: center;">5</td><td style="text-align: center;">5</td><td style="text-align: center;">5</td></tr> </table> </div> <div style="text-align: left;"> <p>$5 + 5 + 5 + 5 = 20$ $4 \times 5 = 20$</p> </div> </div>		6		3	3	20				5	5	5	5
6														
3	3													
20														
5	5	5	5											
<p>Use arrays</p> <p>Encourage children to see that multiplication is commutative.</p>	<p>There are ... rows with ... in each row. There are ... columns with ... in each column.</p> <div style="display: flex; justify-content: space-between;"> <div style="text-align: center;">  <p>3 lots of 5 = 15 $5 + 5 + 5 = 15$</p> </div> <div style="text-align: center;">  <p>5 lots of 3 = 15 $3 + 3 + 3 + 3 + 3 = 15$</p> </div> </div>	<p>I can see ... \times ... and ... \times ...</p> <p style="text-align: center;">$3 \times 5 = 15$ $5 \times 3 = 15$ $3 \times 5 = 5 \times 3$</p>												
<p>Double</p> <p>Encourage children to make links with related facts.</p>	<p>Double ... is ...</p> <div style="display: flex; align-items: center;">  →  </div> <p style="margin-left: 100px;">Double 4 = 4 + 4 Double 4 is 8</p>	<p>Double ... is ... so double ... is ...</p> <div style="display: flex; align-items: center;">  →  </div> <p style="margin-left: 100px;">Double 4 is 8</p> <div style="display: flex; align-items: center;">  →  </div> <p style="margin-left: 100px;">Double 40 is 80</p>												

Progression of skills	Key representations																																									
<p>The 2 times-table</p> <p>Encourage daily counting in multiples both forwards and back. Notice that all multiples of 2 are even numbers.</p>	<p>... lots of 2 =</p> <p>... $\times 2 =$</p> 	<p>... times 2 is equal to ...</p> <table border="1" data-bbox="1467 287 1870 406"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> </table> <p> $1 \times 2 = 2$ $2 = 1 \times 2$ $2 \times 2 = 4$ $4 = 2 \times 2$ $3 \times 2 = 6$ $6 = 3 \times 2$ </p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30										
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<p>The 10 times-table</p> <p>Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.</p>	<p>... lots of 10 =</p> <p>... $\times 10 =$</p> 	<p>... times 10 is equal to ...</p> <table border="1" data-bbox="1467 758 1870 917"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> </table> <p> $1 \times 10 = 10$ $10 = 1 \times 10$ $2 \times 10 = 20$ $20 = 2 \times 10$ $3 \times 10 = 30$ $30 = 3 \times 10$ </p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
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Progression of skills	Key representations																																									
<p>The 5 times-table</p> <p>Encourage daily counting in multiples both forwards and back. Notice the pattern in the numbers.</p>	<p>... lots of 5 =</p> <p>... $\times 5 =$</p>    	<p>... times 5 is equal to ...</p> <table border="1" data-bbox="1456 279 1870 438"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> </table> <p> $1 \times 5 = 5$ $5 = 1 \times 5$ $2 \times 5 = 10$ $10 = 2 \times 5$ $3 \times 5 = 15$ $15 = 3 \times 5$ </p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
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<p>Missing numbers</p> <p>Make links to known facts.</p>	<p>... is equal to ... groups of ...</p> <p>18 socks, how many pairs?</p>  	<p>... times ... is equal to ...</p> <p><input type="text"/> $\times 2 = 18$</p> <p>$18 = 2 \times$ <input type="text"/></p>																																								

Multiplication - Year 3

<p>Year 3</p>	<ul style="list-style-type: none"> Recall and use multiplication facts for the 3, 4 and 8 multiplication tables. Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects. 																															
<p>Progression of skills</p>	<p>Key representations</p>																															
<p>The 3 times-table</p> <p>Encourage daily counting in multiples both forwards and back.</p>	<p>... groups of 3 =</p> <p>... $\times 3 =$</p> <p>3, ... times =</p> <p>$3 \times \dots =$</p> 	<p>... times 3 is equal to ...</p> <table border="1" data-bbox="1422 662 1892 798"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> </table> <p>$4 \times 3 = 12$ $12 = 4 \times 3$</p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
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<p>The 4 times-table</p> <p>Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2 and 4 times-tables.</p>	<p>... groups of 4 =</p> <p>... $\times 4 =$</p> <p>4, ... times =</p> <p>$4 \times \dots =$</p> 	<p>... times 4 is equal to ...</p> <table border="1" data-bbox="1422 1013 1892 1149"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> </table> <p>$3 \times 4 = 12$ $12 = 3 \times 4$</p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
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Progression of skills | **Key representations**

The 8 times-table

Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2, 4 and 8 times-tables.

... lots of 8 =
 $\times 8 =$
 8, ... times =
 $8 \times \dots =$

... times 8 is equal to ...

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30

$3 \times 8 = 24$ $24 = 3 \times 8$

Related facts

Use knowledge of multiplying by 10 to scale times-table facts.

... \times ... ones is equal to ... ones
 so ... \times ... tens is equal to ... tens.

$3 \times 4 = 12$
 $3 \times 40 = 120$

Multiply a 2-digit number by a 1-digit number - no exchange

Children apply their understanding of partitioning to represent and solve calculations using the expanded method.

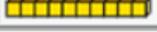
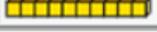
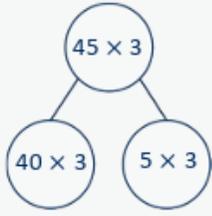
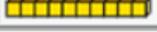
... tens multiplied by ... is equal to ... tens.
 ...ones multiplied by ... is equal to ... ones.

Tens	Ones
30	2
2	2

$30 \times 2 = 60$
 $2 \times 2 = 4$

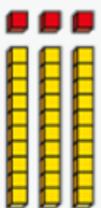
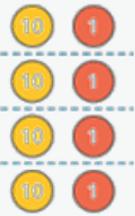
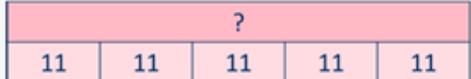
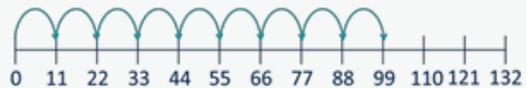
$32 \times 2 = 64$

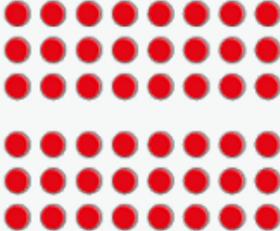
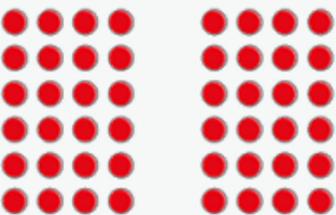
Tens	Ones
20	1
10	1
10	1
10	1
10	1

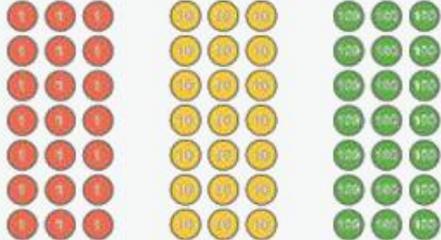
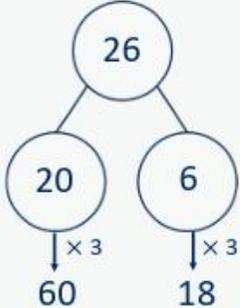
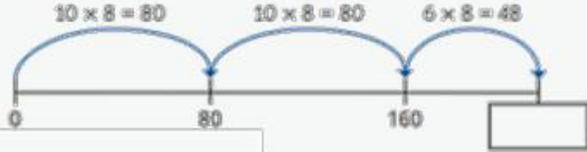
Progression of skills	Key representations																					
<p>Multiply a 2-digit number by a 1-digit number - with exchange</p> <p>Children apply their understanding of partitioning to represent and solve calculations using the expanded method.</p>	<p>... tens multiplied by ... is equal to ... tens. ... ones multiplied by ... is equal to ... ones.</p> <table border="1" data-bbox="683 335 1030 662"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table> <p>$20 \times 4 = 80$ $4 \times 4 = 16$</p> <p>$24 \times 4 = 96$</p>	Tens	Ones											<div data-bbox="1344 430 1556 646">  </div> <table border="1" data-bbox="1585 443 1966 635"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>	Tens	Ones						
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<p>Scaling</p> <p>Children focus on multiplication as scaling (... times the size) as opposed to repeated addition.</p>	<p>There are times as many ... as ...</p> <div data-bbox="683 861 1288 1013">  </div> <p>There are 3 times as many triangles as circles.</p>	<p>... is ... times the size of is ... times the length/height of ...</p> <div data-bbox="1355 821 1792 901">  </div> <div data-bbox="1836 861 2004 1117">  </div> <p>Miss Smith is twice the height of Jo.</p>																				

Progression of skills	Key representations								
<p>Correspondence problems (How many ways?)</p> <p>Encourage children to work systematically to find all the different possible combinations.</p>	<p>For every ... , there are ... possible ... There are ... × ... possibilities altogether.</p> <div style="display: flex; align-items: center; justify-content: center;">  <table border="1" data-bbox="1093 320 1379 663" style="margin: 0 20px;"> <thead> <tr> <th data-bbox="1093 320 1234 357">hats</th> <th data-bbox="1234 320 1379 357">scarves</th> </tr> </thead> <tbody> <tr> <td data-bbox="1093 357 1234 459">blue </td> <td data-bbox="1234 357 1379 459">   </td> </tr> <tr> <td data-bbox="1093 459 1234 561">orange </td> <td data-bbox="1234 459 1379 561">   </td> </tr> <tr> <td data-bbox="1093 561 1234 663">purple </td> <td data-bbox="1234 561 1379 663">   </td> </tr> </tbody> </table> </div> <p>For every hat, there are two possible scarves. $3 \times 2 = 6$</p> <p>There are 6 possibilities altogether.</p>	hats	scarves	blue 	 	orange 	 	purple 	 
hats	scarves								
blue 	 								
orange 	 								
purple 	 								

Multiplication - Year 4

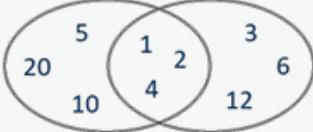
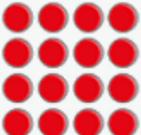
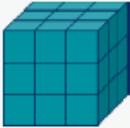
<p>Year 4</p>	<ul style="list-style-type: none"> Recall multiplication facts for multiplication tables up to 12×12 Use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together three numbers. Recognise and use factor pairs and commutativity in mental calculations. Multiply two-digit and three-digit numbers by a one-digit number using formal written layout. Solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects. 																																																																																																					
<p>Progression of skills</p>	<p>Key representations</p>																																																																																																					
<p>Times-table facts to 12×12</p> <p>Encourage daily counting in multiples both forwards and back. Encourage children to notice links between related times-tables.</p>	<p>... groups of ... =</p> <p>... times ... is equal to ...</p> <p>... \times ... =</p>    	<table border="1" data-bbox="1646 702 1960 1005"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> <tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr> <tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr> <tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr> <tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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<p>Multiply by 1 and 0</p>	<p>Any number multiplied by 1 is equal to ...</p> <p>Any number multiplied by 0 is equal to ...</p>  	<p>... \times ... = ...</p> <table data-bbox="1467 1117 1836 1284"> <tr> <td>$1 \times 1 = 1$</td> <td>$1 \times 0 = 0$</td> </tr> <tr> <td>$2 \times 1 = 2$</td> <td>$2 \times 0 = 0$</td> </tr> <tr> <td>$3 \times 1 = 3$</td> <td>$3 \times 0 = 0$</td> </tr> <tr> <td>$4 \times 1 = 4$</td> <td>$4 \times 0 = 0$</td> </tr> </table>	$1 \times 1 = 1$	$1 \times 0 = 0$	$2 \times 1 = 2$	$2 \times 0 = 0$	$3 \times 1 = 3$	$3 \times 0 = 0$	$4 \times 1 = 4$	$4 \times 0 = 0$																																																																																												
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Progression of skills	Key representations																													
<p>Multiply 3 numbers</p> <p>Children use their understanding of commutativity to multiply more efficiently.</p>	<p>To work out ... \times ... \times ..., I can first calculate ... \times ... and then multiply the answer by ...</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> $4 \times 2 \times 3 = 8 \times 3 = 24$ $2 \times 3 \times 4 = 6 \times 4 = 24$ $3 \times 4 \times 2 = 12 \times 2 = 24$ </div> </div>																													
<p>Factor pairs</p> <p>Children explore equivalent calculations using different factors pairs.</p>	<p>$12 = \dots \times \dots$, so ... $\times 12 = \dots \times \dots \times \dots$</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$8 \times 6 = 8 \times 3 \times 2$ $8 \times 6 = 24 \times 2$</p> </div> <div style="text-align: center;">  <p>$6 \times 8 = 6 \times 4 \times 2$ $6 \times 8 = 24 \times 2$</p> </div> </div>																													
<p>Multiply by 10 and 100</p> <p>Some children may over-generalise that multiplying by 10 or 100 always results in adding zeros. This will cause issues later when multiplying decimals.</p>	<p>When I multiply by 10, the digits move ... place value column to the left. ... is 10 times the size of ...</p> <div style="display: flex; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center; width: 100px;"> <tr><th style="width: 33px;">H</th><th style="width: 33px;">T</th><th style="width: 33px;">O</th></tr> <tr><td> </td><td>●●</td><td>●●●</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center; width: 100px;"> <tr><th style="width: 33px;">H</th><th style="width: 33px;">T</th><th style="width: 33px;">O</th></tr> <tr><td>●●</td><td>●●●</td><td> </td></tr> </table> <div style="margin-left: 20px;"> $35 \times 10 = 350$ </div> </div>	H	T	O		●●	●●●	H	T	O	●●	●●●		<p>When I multiply by 100, the digits move ... place value columns to the left. ... is 100 times the size of ...</p> <div style="display: flex; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center; width: 150px;"> <tr><th style="width: 37.5px;">Th</th><th style="width: 37.5px;">H</th><th style="width: 37.5px;">T</th><th style="width: 37.5px;">O</th></tr> <tr><td> </td><td> </td><td>●</td><td>●●●</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center; width: 150px;"> <tr><th style="width: 37.5px;">Th</th><th style="width: 37.5px;">H</th><th style="width: 37.5px;">T</th><th style="width: 37.5px;">O</th></tr> <tr><td>●</td><td>●●●</td><td> </td><td> </td></tr> </table> <div style="margin-left: 20px;"> $14 \times 100 = 1,400$ </div> </div>	Th	H	T	O			●	●●●	Th	H	T	O	●	●●●		
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Progression of skills	Key representations
<p>Related facts</p> <p>Use knowledge of multiplying by 10 and 100 to scale times-table facts.</p>	<p>... × ... ones is equal to ... ones so ... × ... tens is equal to ... tens and ... × ... hundreds is equal to ... hundreds.</p>  <p> $3 \times 7 = 21$ $7 \times 3 = 21$ $3 \times 70 = 210$ $7 \times 30 = 210$ $3 \times 700 = 2,100$ $7 \times 300 = 2,100$ </p>
<p>Mental strategies</p> <p>Partition 2 or 3-digit numbers to multiply using informal methods.</p>	<p>... tens multiplied by ... is equal to ... tens. ...ones multiplied by ... is equal to ... ones.</p>    <p> $3 \times 26 = 60 + 18 = 78$ $26 \times 8 = 80 + 80 + 48 = 208$ </p>

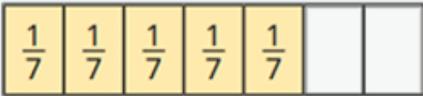
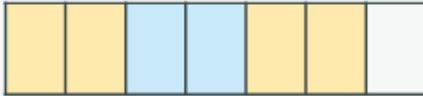
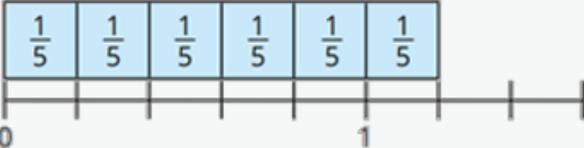
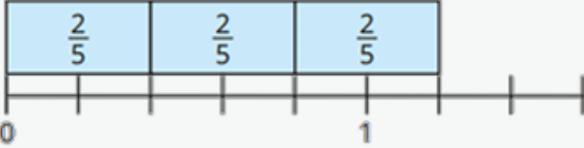
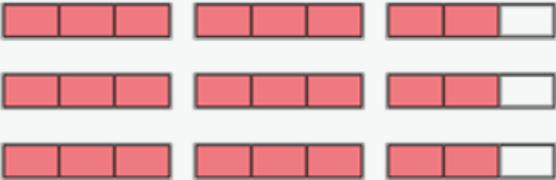
Progression of skills	Key representations																								
<p>Multiply a 2 or 3-digit number by a 1-digit number</p> <p>The short multiplication method is introduced for the first time, initially in an expanded form.</p>	<p>To multiply a 2-digit number by ... , I multiply the ones by ... and the tens by ... To multiply a 3-digit number by ... , I multiply the ones by ... , the tens by ... and the hundreds by ...</p>																								
<p>Scaling</p> <p>Children focus on multiplication as scaling (... times the size).</p>	<p>... is ... times the size of ...</p> <div style="display: flex; justify-content: space-around;"> <div data-bbox="674 738 1077 850"> <p>7</p> <p>7 7 7 7 7 7</p> <p>A computer mouse costs £7 A keyboard costs 6 times as much.</p> </div> <div data-bbox="1391 738 1861 850"> <p>6</p> <p>6 6 6 6 6 6 6</p> <p>A red ribbon is 6 cm. A yellow ribbon is 7 times as long.</p> </div> </div>																								
<p>Correspondence problems</p> <p>Encourage children to use tables to show all the different possible combinations.</p>	<p>For every ... , there are ... possibilities. There are ... × ... possibilities altogether.</p> <p>A pizza company offers a choice of 5 toppings and 3 bases.</p> <p>$5 \times 3 = 15$</p> <table border="1" data-bbox="1283 1018 2013 1265"> <thead> <tr> <th></th> <th>Deep pan</th> <th>Italian</th> <th>Thin</th> </tr> </thead> <tbody> <tr> <th>Cheese</th> <td>C DP</td> <td>C I</td> <td>C Th</td> </tr> <tr> <th>Mushroom</th> <td>M DP</td> <td>M I</td> <td>M Th</td> </tr> <tr> <th>Vegetable</th> <td>V DP</td> <td>V I</td> <td>V Th</td> </tr> <tr> <th>Chicken</th> <td>C DP</td> <td>C I</td> <td>C Th</td> </tr> <tr> <th>Tuna</th> <td>T DP</td> <td>T I</td> <td>T Th</td> </tr> </tbody> </table>		Deep pan	Italian	Thin	Cheese	C DP	C I	C Th	Mushroom	M DP	M I	M Th	Vegetable	V DP	V I	V Th	Chicken	C DP	C I	C Th	Tuna	T DP	T I	T Th
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Multiplication - Year 5

<p>Year 5</p>	<ul style="list-style-type: none"> Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers Recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³) Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers. Multiply numbers mentally drawing upon known facts. Multiply whole numbers and those involving decimals by 10, 100 and 1000 Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams. 																																
<p>Progression of skills</p>	<p>Key representations</p>																																
<p>Multiples and factors</p> <p>Encourage children to notice patterns and make links with known facts.</p>	<p>... is a multiple of ... because ... × ... = ...</p>  <table border="1" data-bbox="674 906 1099 1027"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	<p>... is a factor of ... because ... × ... = ...</p>  1×8  2×4 <p>1, 2, 4 and 8 are factors of 8</p>	<p>The common factors of ... and ... are ...</p> <p>Factors of 20 Factors of 12</p> 
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<p>Square and cube numbers</p>	<p>... squared means ... × ...</p>  $1 \times 1 = 1$  $2^2 = 4$  $3^2 = 9$  $4^2 = 16$		<p>... cubed means ... × ... × ...</p>  $1^3 = 1$  $2^3 = 8$  $3^3 = 27$																														

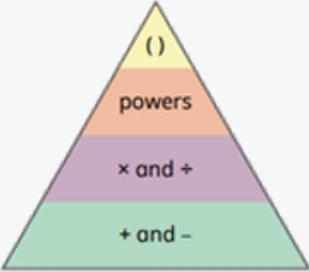
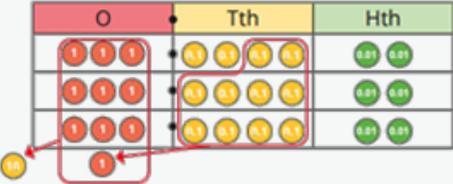
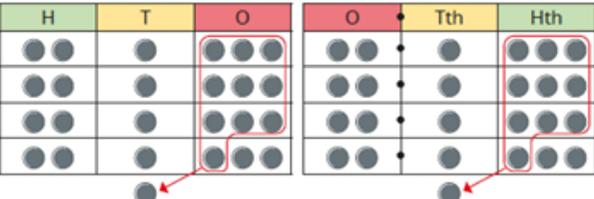
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<p>Multiply numbers up to 4 digits by a 1-digit number</p> <p>This builds on the short multiplication method introduced in Y4</p>	<p>To multiply a 4-digit number by ... , I multiply the ones by ... , the tens by ... , the hundreds by ... and the thousands by ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr> <th style="width: 20px;">Th</th> <th style="width: 20px;">H</th> <th style="width: 20px;">T</th> <th style="width: 20px;">O</th> </tr> <tr> <td>1000</td> <td>900</td> <td>10 10 10 10 10</td> <td>1 1</td> </tr> <tr> <td>1000</td> <td>900</td> <td>10 10 10 10 10</td> <td>1 1</td> </tr> <tr> <td>1000</td> <td>900</td> <td>10 10 10 10 10</td> <td>1 1</td> </tr> </table> <table border="1" style="border-collapse: collapse; text-align: center; margin-left: 20px;"> <tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td>1</td><td>1</td><td>5</td><td>2</td></tr> <tr><td>×</td><td> </td><td> </td><td> </td><td> </td><td>3</td></tr> <tr><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td></tr> </table> </div>		Th	H	T	O	1000	900	10 10 10 10 10	1 1	1000	900	10 10 10 10 10	1 1	1000	900	10 10 10 10 10	1 1								1	1	5	2	×					3																																
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<p>Multiply numbers up to 4 digits by a 2-digit number</p> <p>Numbers are first partitioned using an area model then long multiplication is introduced for the first time.</p>	<p>I can partition ... into ... and ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr> <td>×</td> <td>10 10 10</td> <td>10 10 10</td> </tr> <tr> <td>30</td> <td>300</td> <td>90</td> </tr> <tr> <td>2</td> <td>20</td> <td>6</td> </tr> </table> <table border="1" style="border-collapse: collapse; text-align: center; margin-left: 20px;"> <tr> <td>×</td> <td>40</td> <td>4</td> </tr> <tr> <td>30</td> <td>1,200</td> <td>120</td> </tr> <tr> <td>2</td> <td>80</td> <td>8</td> </tr> </table> </div> <p>$32 \times 44 = 1,200 + 80 + 120 + 8$ $32 \times 44 = 1,408$</p>	×	10 10 10	10 10 10	30	300	90	2	20	6	×	40	4	30	1,200	120	2	80	8	<p>First, I multiply by the ... Then I multiply by the ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr> <td>×</td> <td>10</td> <td>3</td> </tr> <tr> <td>30</td> <td>300</td> <td>90</td> </tr> <tr> <td>2</td> <td>20</td> <td>6</td> </tr> </table> <table border="1" style="border-collapse: collapse; text-align: center; margin-left: 20px;"> <tr><td> </td><td> </td><td> </td><td> </td><td> </td></tr> <tr><td> </td><td> </td><td>3</td><td>2</td><td> </td></tr> <tr><td>×</td><td> </td><td> </td><td>1</td><td>3</td></tr> <tr><td> </td><td> </td><td> </td><td>9</td><td>6</td></tr> <tr><td> </td><td> </td><td> </td><td>3</td><td>2</td><td>0</td></tr> <tr><td> </td><td> </td><td> </td><td>4</td><td>1</td><td>6</td></tr> <tr><td> </td><td> </td><td> </td><td> </td><td> </td><td> </td></tr> </table> <div style="margin-left: 20px;"> <p>(32 × 3)</p> <p>(32 × 10)</p> </div> </div> <p style="text-align: center; margin-top: 10px;">$300 + 90 + 20 + 6 = 416$</p>	×	10	3	30	300	90	2	20	6								3	2		×			1	3				9	6				3	2	0				4	1	6						
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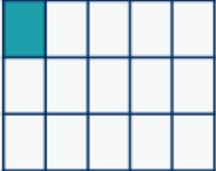
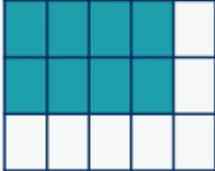
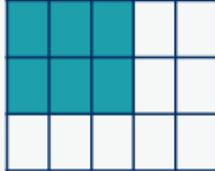
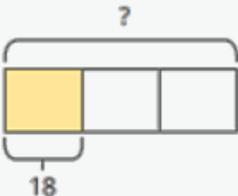
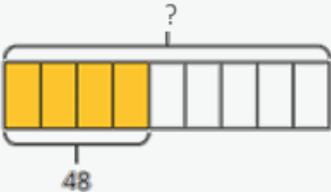
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<p>Mental strategies</p> <p>Children continue to use efficient mental strategies such as partitioning and knowledge of factor pairs and related facts to multiply.</p>	<p>The most efficient strategy to calculate ... \times ... is ... To calculate ... \times 12, I can do ... \times ... \times ...</p> <p>For example: 121×12 I could calculate 100×12 plus 20×12 plus 1×12 I could calculate 121×10 plus 121×2 I could calculate $121 \times 6 \times 2$ I could calculate $121 \times 4 \times 3$</p>																																							

Progression of skills	Key representations
<p>Multiply fractions by a whole number</p> <p>Make links with repeated addition.</p> <p>E.g. $\frac{1}{5} \times 4 = \frac{1}{5} + \frac{1}{5} + \frac{1}{5} + \frac{1}{5}$</p>	<p>To multiply a fraction by an integer, I multiply the numerator by the integer and the denominator remains the same.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  $\frac{1}{7} \times 5 = \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} + \frac{1}{7} = \frac{5}{7}$ </div> <div style="text-align: center;">  $\frac{2}{7} \times 3 = \frac{2}{7} + \frac{2}{7} + \frac{2}{7} = \frac{6}{7}$ </div> </div> <div style="display: flex; justify-content: space-around; margin-top: 20px;"> <div style="text-align: center;">  $\frac{1}{5} \times 6 = \frac{6}{5} = 1\frac{1}{5}$ </div> <div style="text-align: center;">  $\frac{2}{5} \times 3 = \frac{6}{5} = 1\frac{1}{5}$ </div> </div>
<p>Multiply mixed numbers by a whole number</p>	<p>I can partition $\frac{\square}{\square}$ into \square and $\frac{\square}{\square}$</p> <div style="display: flex; align-items: center; margin-top: 10px;"> <div style="margin-right: 20px;">  </div> <div> $2\frac{2}{3} \times 3$ $2 \times 3 = 6 \quad \frac{2}{3} \times 3 = \frac{6}{3} = 2$ $2\frac{2}{3} \times 3 = 6 + 2 = 8$ </div> </div>

Multiplication - Year 6

Year 6	<ul style="list-style-type: none"> Identify common factors and common multiples. Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication. Multiply numbers by 10, 100 and 1,000 Multiply one-digit numbers with up to two decimal places by whole numbers. Use their knowledge of the order of operations to carry out calculations involving the 4 operations. Multiply simple pairs of proper fractions, writing the answer in its simplest form. Solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts. Solve problems involving the calculation of percentages. 																																																	
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Multiply numbers up to 4 digits by a 2-digit number	<p>To multiply by a 2-digit number, first multiply by the ones, then multiply by the tens and then find the total.</p> <div style="text-align: right;"> <table border="1" style="border-collapse: collapse; margin-left: auto;"> <tr><td></td><td></td><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td>1</td><td>2</td><td>0</td><td>7</td><td></td></tr> <tr><td>×</td><td></td><td></td><td></td><td>3</td><td>6</td><td></td></tr> <tr><td>+</td><td></td><td>7</td><td>2</td><td>4</td><td>2</td><td>(1,207 × 6)</td></tr> <tr><td></td><td>3</td><td>6</td><td>2</td><td>1</td><td>0</td><td>(1,207 × 30)</td></tr> <tr><td></td><td>4</td><td>3</td><td>4</td><td>5</td><td>2</td><td></td></tr> <tr><td></td><td>1</td><td></td><td></td><td></td><td></td><td></td></tr> </table> </div>										1	2	0	7		×				3	6		+		7	2	4	2	(1,207 × 6)		3	6	2	1	0	(1,207 × 30)		4	3	4	5	2			1					
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Progression of skills	Key representations																															
<p>Order of operations</p> <p>Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  <p>$(3 + 4) \times 2 = 14$</p> </div> <div style="text-align: center;">  <p>$3 + 4^2 = 19$</p> </div> <div style="text-align: center;">  <p>$3 + 4 \times 2 = 11$</p> </div> </div>																															
<p>Multiply decimals by integers</p> <p>This is the first time children multiply decimals by numbers other than 10, 100 or 1,000. Encourage them to make links with known facts and whole number multiplication.</p>	<p>I know that ... \times ... = ..., so I also know that ... \times ... = ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$6 \times 2 = 12$</p> </div> <div style="text-align: center;">  <p>$6 \times 0.2 = 1.2$</p> </div> </div>	<p>I need to exchange 10 ... for 1 ...</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$213 \times 4 = 852$</p> </div> <div style="text-align: center;">  <p>$2.13 \times 4 = 8.52$</p> </div> </div> <div style="text-align: right; margin-top: 10px;"> <table border="1" style="border-collapse: collapse;"> <tr><td></td><td></td><td></td><td></td><td></td></tr> <tr><td></td><td></td><td>3</td><td>4</td><td>2</td></tr> <tr><td></td><td>\times</td><td></td><td></td><td>3</td></tr> <tr><td></td><td></td><td>1</td><td>0</td><td>2</td></tr> <tr><td></td><td></td><td></td><td></td><td>6</td></tr> <tr><td></td><td></td><td></td><td></td><td>0</td></tr> </table> </div>								3	4	2		\times			3			1	0	2					6					0
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Progression of skills	Key representations	
<p>Multiply fractions by fractions</p> <p>Encourage children to give answers in their simplest form.</p>	<p>When multiplying a pair of fractions, I need to multiply the numerator and multiply the denominator.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  $\frac{1}{3} \times \frac{1}{5} = \frac{1}{15}$ </div> <div style="text-align: center;">  $\frac{2}{3} \times \frac{4}{5} = \frac{8}{15}$ </div> <div style="text-align: center;">  $\frac{2}{3} \times \frac{3}{5} = \frac{6}{15} = \frac{2}{5}$ </div> </div>	
<p>Find the whole</p> <p>Children multiply to find the whole from a given part.</p>	<p>If $\frac{1}{\square}$ is ... , then the whole is ... \times ...</p> <p>$\frac{1}{3}$ of ___ = 18</p>  <p>$18 \times 3 = 54$</p> <p>$\frac{1}{3}$ of 54 = 18</p>	<p>If $\frac{\square}{\square}$ is ... , then $\frac{1}{\square}$ is ... and the whole is ... \times ...</p> <p>$\frac{4}{9}$ of ___ = 48</p>  <p>$\frac{1}{9} = 48 \div 4 = 12$</p> <p>$9 \times 12 = 108$</p> <p>$\frac{4}{9}$ of 108 = 48</p>

Progression of skills	Key representations																																	
<p>Calculate percentages</p> <p>Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.</p>	<p>There are ... lots of ... % in 100%</p> <p>To find ... %, I need to divide by ...</p> <table border="1" data-bbox="680 325 1178 432"> <tr><td colspan="4">100%</td></tr> <tr><td colspan="2">50%</td><td colspan="2">50%</td></tr> <tr><td>25%</td><td>25%</td><td>25%</td><td>25%</td></tr> </table> <p>50% of ... = ... ÷ 2</p> <p>25% of ... = ... ÷ 4</p>	100%				50%		50%		25%	25%	25%	25%	<p>... % is made up of ... %, and ... %</p> <table border="1" data-bbox="1236 309 1977 397"> <tr><td colspan="10">100%</td></tr> <tr><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td></tr> </table> <p>To find 30%, I can find 10% and then multiply it by 3</p> <p>To find 23%, I can use 10% × 2 and 1% × 3</p> <p>To find 99%, I can find 1%, then subtract from 100%</p>	100%										10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
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<p>Calculations involving ratio</p> <p>Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent. Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.</p>	<p>For every ... , there are ...</p> <p>For every 1 adult on a school trip, there are 6 children.</p> <p>adults </p> <p>children </p> <table border="1" data-bbox="1576 715 1895 906"> <thead> <tr><th>Adults</th><th>Children</th></tr> </thead> <tbody> <tr><td>1</td><td>6</td></tr> <tr><td>2</td><td>12</td></tr> <tr><td>3</td><td>18</td></tr> </tbody> </table> <p>The ratio of adults to children is 1 : 6</p> <table border="1" data-bbox="1456 1075 1971 1225"> <tr><td>Adults</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr><td>Children</td><td>0</td><td>6</td><td>12</td><td>18</td><td></td><td></td><td></td></tr> </table>		Adults	Children	1	6	2	12	3	18	Adults	0	1	2	3	4	5	6	Children	0	6	12	18											
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Progression of Skills - Division

Year group	Skill
Nursery	<ul style="list-style-type: none">• Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)
Reception	<ul style="list-style-type: none">• Sharing• Grouping
Year 1	<ul style="list-style-type: none">• Make equal groups – grouping• Make equal groups – sharing• Find a half• Find a quarter

Year group	Skill
Year 2	<ul style="list-style-type: none">• Divide by 2• Divide by 10• Divide by 5• Missing numbers• Unit fractions• Non-unit fractions
Year 3	<ul style="list-style-type: none">• Divide by 3• Divide by 4• Divide by 8• Related facts• Divide a 2-digit number by a 1-digit number - no exchange• Divide a 2-digit number by a 1-digit number - with remainders• Unit fractions of a set of objects• Non-unit fractions of a set of objects

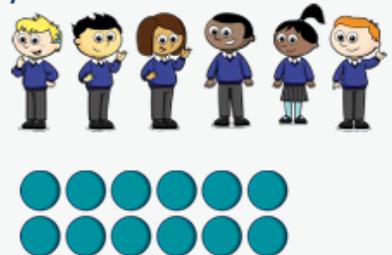
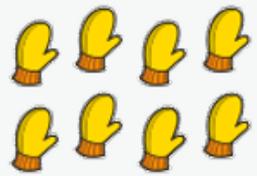
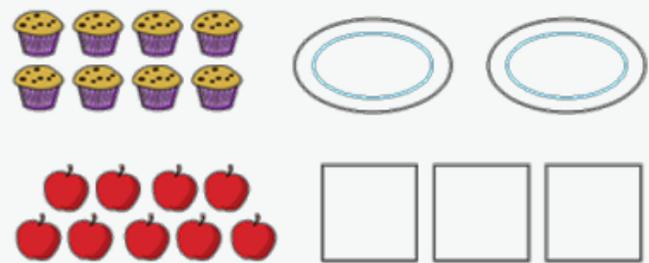
Year group	Skill
Year 4	<ul style="list-style-type: none">• Division facts to 12×12• Divide a number by 1 and itself• Related facts• Divide a 2 or 3-digit number by a 1-digit number• Divide by 10 and 100
Year 5	<ul style="list-style-type: none">• Mental strategies• Divide numbers up to 4 digits by a 1-digit number• Divide by 10, 100 and 1,000• Fraction of an amount

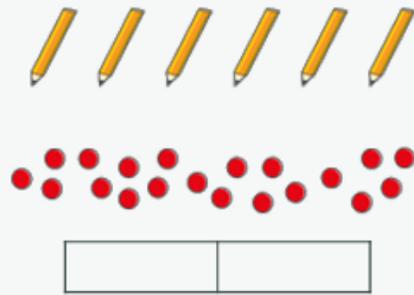
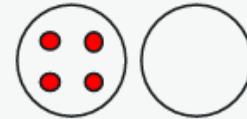
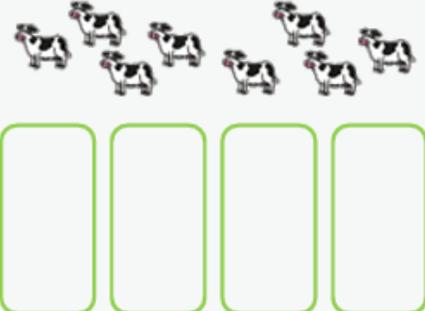
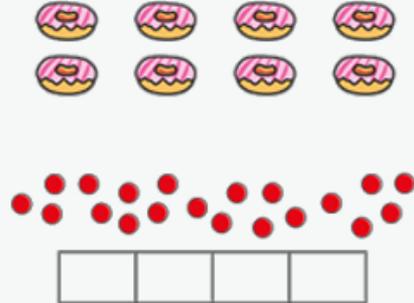
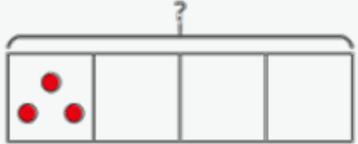
Year group	Skill
Year 6	<ul style="list-style-type: none"><li data-bbox="618 236 904 268">• Short division<li data-bbox="618 320 965 352">• Mental strategies<li data-bbox="618 405 891 437">• Long division<li data-bbox="618 489 1010 521">• Order of operations<li data-bbox="618 574 1137 606">• Divide by 10, 100 and 1,000<li data-bbox="618 659 1128 691">• Divide decimals by integers<li data-bbox="618 743 1223 775">• Decimal and fraction equivalents<li data-bbox="618 828 1173 860">• Divide a fraction by an integer<li data-bbox="618 912 1048 944">• Fraction of an amount<li data-bbox="618 997 1039 1029">• Calculate percentages<li data-bbox="618 1082 1122 1114">• Calculations involving ratio

Division - Reception

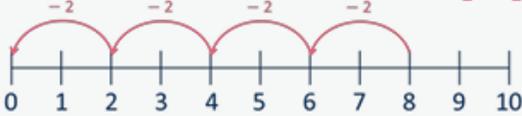
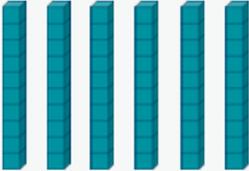
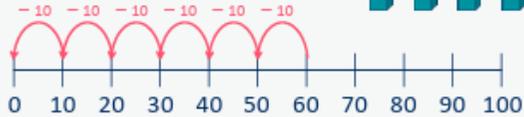
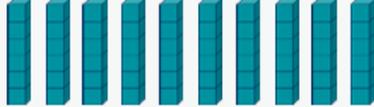
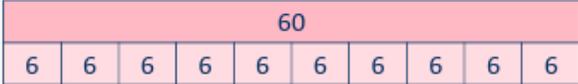
<p>Reception</p>	<ul style="list-style-type: none"> • Have a deep understanding of number to 10, including the composition of each number. • Subitise (recognise quantities without counting) up to 5 • Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 and some number bonds to 10, including double facts. • Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.
<p>Progression of skills</p>	<p>Key representations</p>
<p>Sharing</p> <p>Provide practical activities such as sharing items during snack time. Encourage children to check whether items have been shared fairly (equally).</p>	<p>There are ... altogether. They are shared equally between ... groups.</p> 
<p>Grouping</p> <p>Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.</p>	<p>There are ... groups of ... There are ... altogether.</p> 

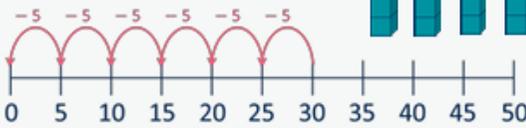
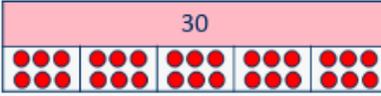
Division - Year 1

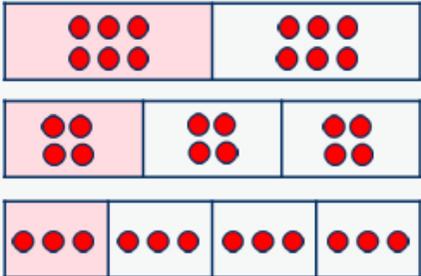
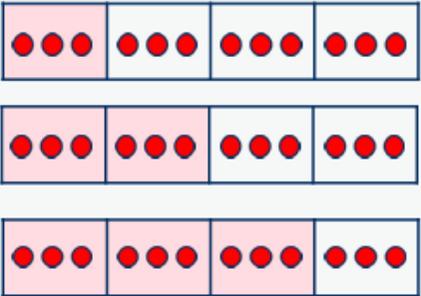
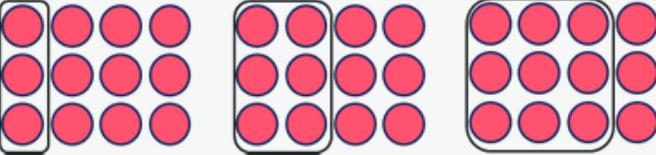
<p>Year 1</p>	<ul style="list-style-type: none"> Solve simple one-step problems involving division, using concrete objects, pictorial representations and arrays with the support of the teacher. Recognise, find and name a half as one of two equal parts of a quantity. Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity. 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Make equal groups - grouping</p> <p>Encourage children to physically move objects into equal groups. They can also circle equal groups when using pictures.</p>	<p>There are ... altogether. How many groups of ... can you make?</p> 	<p>Circle groups of 2 There are ... groups of 2</p> 	<p>Take ... cubes. Make equal groups.</p>  <p>There are ... groups of ...</p>
<p>Make equal groups – sharing</p> <p>Encourage children to check that the objects have been shared fairly and each group is the same.</p>	<p>... have been shared equally between... There are ... on/in each ...</p> 		<p>Take ... cubes. Share them between ...</p>  <p>12 shared between ... is ...</p>

Progression of skills	Key representations		
<p>Find a half</p> <p>Start with practical opportunities to share a quantity into 2 groups. Progress to circling half of the objects in a picture and then to finding the whole from a given half.</p>	<p>To find half, I need to share into 2 equal groups.</p>  <p>There are ... in each group.</p>	<p>Half of ... is ...</p> 	<p>If ... is half, what is the whole?</p>  <p>4 is half of ...</p>
<p>Find a quarter</p> <p>Start with practical opportunities to share a quantity into 4 groups. Progress to using pictures or bar models to find a quarter and then to finding the whole from a given quarter.</p>	<p>To find a quarter, I need to share into 4 equal groups.</p>  <p>There are ... in each group.</p>	<p>A quarter of ... is ...</p> 	<p>If ... is one quarter, what is the whole?</p>  <p>3 is one quarter of ...</p>

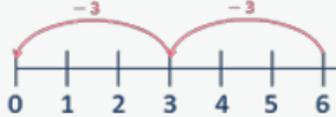
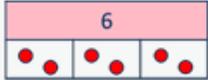
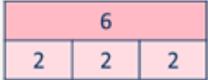
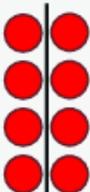
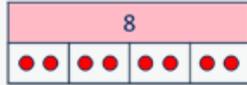
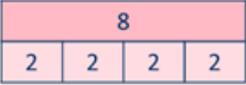
Division - Year 2

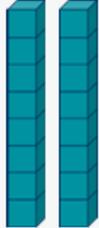
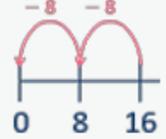
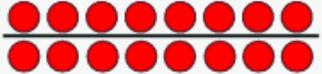
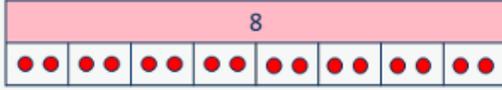
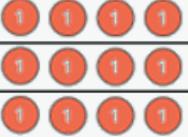
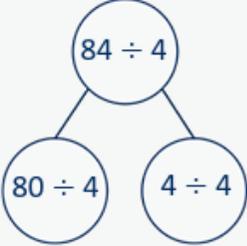
Year 2	<ul style="list-style-type: none"> Recall and use division facts for the 2, 5 and 10 multiplication tables. Calculate mathematical statements for division within the multiplication tables and write them using the division (\div) and equals ($=$) signs. Recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$ and $\frac{3}{4}$ of a quantity. 	
Progression of skills	Key representations	
<p>Divide by 2</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts and halving.</p>	<p>There are ... equal groups of 2 $\dots \div 2 = \dots$</p>  <p>$4 \times 2 = 8$ $8 \div 2 = 4$</p>  	<p>... shared equally between 2 is ... Half of ... is ... $\dots \div 2 = \dots$</p>  <p>$4 \times 2 = 8$ $8 \div 2 = 4$</p>  
<p>Divide by 10</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... equal groups of 10 $\dots \div 10 = \dots$</p> <p>$6 \times 10 = 60$ $60 \div 10 = 6$</p>  	<p>... shared equally between 10 is ... $\dots \div 10 = \dots$</p> <p>$6 \times 10 = 60$ $60 \div 10 = 6$</p>  

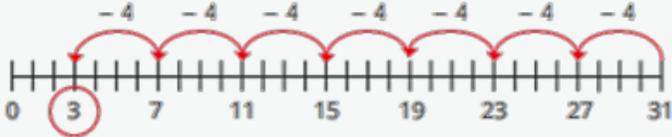
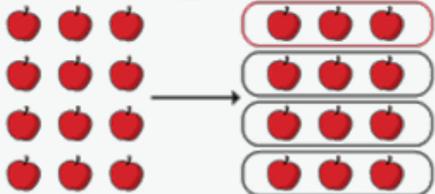
Progression of skills	Key representations																					
<p>Divide by 5</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... equal groups of 5</p> <p>... $\div 5 = \dots$</p>  <p>$6 \times 5 = 30$ $30 \div 5 = 6$</p>  	<p>... shared equally between 5 is ...</p> <p>... $\div 5 = \dots$</p>  <p>$6 \times 5 = 30$ $30 \div 5 = 6$</p>  																				
<p>Missing numbers</p> <p>Bar models are useful to show the link between multiplication and division.</p>	<p>... divided by 2/5/10 is equal to ...</p> <table border="1" data-bbox="683 766 862 845"> <tr><td>?</td></tr> <tr><td>10</td><td>10</td></tr> </table> $\square \div 2 = 10$ <table border="1" data-bbox="683 869 1108 949"> <tr><td>?</td></tr> <tr><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td></tr> </table> $\square \div 5 = 10$ <table border="1" data-bbox="683 973 1444 1053"> <tr><td>?</td></tr> <tr><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td><td>10</td></tr> </table> $\square \div 10 = 10$?	10	10	?	10	10	10	10	10	?	10	10	10	10	10	10	10	10	10	10
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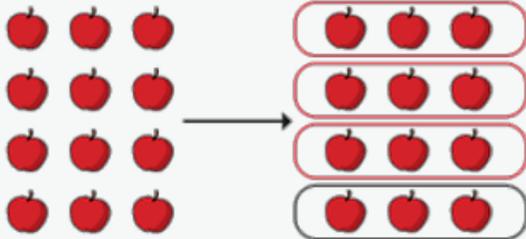
Progression of skills	Key representations	
<p>Unit fractions</p> <p>In Y2 the focus is on finding $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{3}$</p> <p>Bar models are useful to show the link between division and finding a fraction.</p>	<p>The objects have been shared fairly into ... groups.</p> <p>$\frac{1}{\square}$ of ... is ...</p> 	<p>There are ... equal parts.</p> <p>There is ... part circled.</p> <p>$\frac{1}{\square}$ is circled.</p> 
<p>Non-unit fractions</p> <p>In Y2 the focus is on finding $\frac{2}{4}$ and $\frac{3}{4}$</p> <p>Prompt children to notice that $\frac{2}{4}$ is equivalent to $\frac{1}{2}$</p>	<p>The objects have been shared fairly into ... groups.</p> <p>$\frac{\square}{\square}$ of ... is ...</p> 	<p>There are ... equal parts.</p> <p>There are ... parts circled.</p> <p>$\frac{\square}{\square}$ is circled.</p> 

Division - Year 3

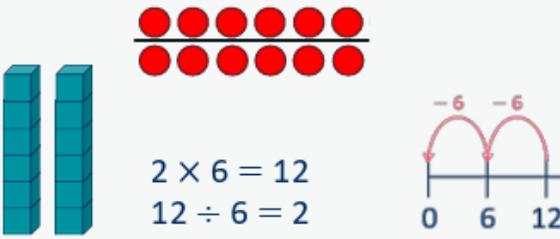
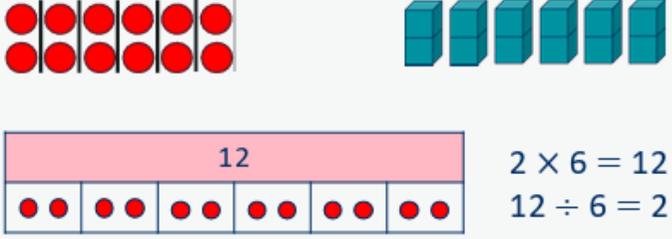
<p>Year 3</p>	<ul style="list-style-type: none"> Recall and use division facts for the 3, 4 and 8 multiplication tables. Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods. Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Divide by 3</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... groups of 3 in ...</p> <p>... $\div 3 =$</p>  <p>$2 \times 3 = 6$ $6 \div 3 = 2$</p>  	<p>... has been shared equally into 3 equal groups.</p> <p>... $\div 3 =$</p>  <p>$2 \times 3 = 6$ $6 \div 3 = 2$</p>   
<p>Divide by 4</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... groups of 4 in ...</p> <p>... $\div 4 =$</p>  <p>$2 \times 4 = 8$ $8 \div 4 = 2$</p>  	<p>... has been shared equally into 4 equal groups.</p> <p>... $\div 4 =$</p>  <p>$2 \times 4 = 8$ $8 \div 4 = 2$</p>   

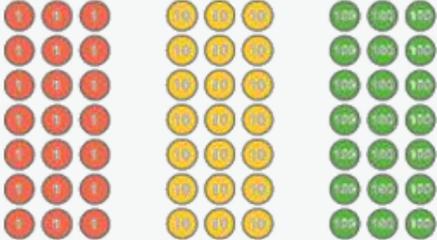
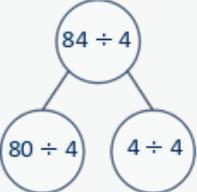
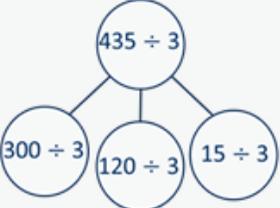
Progression of skills	Key representations																	
<p>Divide by 8</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... groups of 8 in ... $\dots \div 8 =$</p>  <p>$2 \times 8 = 16$ $16 \div 8 = 2$</p>  	<p>... has been shared equally into 8 equal groups. $\dots \div 8 =$</p>    <p>$2 \times 8 = 16$ $16 \div 8 = 2$</p>																
<p>Related facts</p> <p>Link to known times-table facts.</p>	<p>... \div ... is equal to ..., so ... tens \div ... is equal to ... tens.</p>     <p>$12 \div 3 = 4$ $120 \div 3 = 40$</p>																	
<p>Divide a 2-digit number by a 1-digit number - no exchange</p> <p>Partition into tens and ones to divide and then recombine.</p>	<p>... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones.</p> <table border="1" data-bbox="689 1002 1012 1225"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table> <p>$60 \div 2 = 30$ $4 \div 2 = 2$ $64 \div 2 = 32$</p>  <table border="1" data-bbox="1639 1008 1975 1225"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>		Tens	Ones					Tens	Ones								
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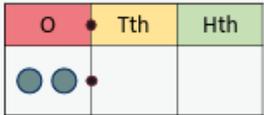
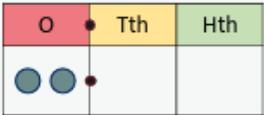
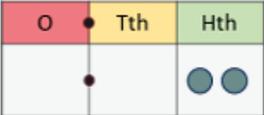
Progression of skills	Key representations																																					
<p>Divide a 2-digit number by a 1-digit number - with remainders</p> <p>Encourage children to partition numbers flexibly to help them to divide more efficiently.</p>	<p>... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones.</p> <table border="1" data-bbox="689 448 1039 772"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> </tbody> </table> <div data-bbox="1070 432 1267 632"> $96 \div 4$ $80 \div 4 \quad 16 \div 4$ </div> <p> $80 \div 4 = 20$ $16 \div 4 = 4$ $96 \div 4 = 24$ </p>	Tens	Ones											<p>There are ... groups of ... There are ... remaining.</p> <p>$31 \div 4 = 7 \text{ r}3$</p>  <p>$94 \div 4 = 23 \text{ r}2$</p> <table border="1" data-bbox="1339 596 1541 783"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> </tbody> </table>  <table border="1" data-bbox="1749 596 1951 783"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> <tr><td></td><td></td></tr> </tbody> </table>	Tens	Ones											Tens	Ones										
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<p>Unit fractions of a set of objects</p> <p>Bar models are useful to show the link between division and fractions, for example, dividing by 3 and finding a third.</p>	<p>The whole is divided into ... equal parts. Each part is $\frac{1}{\square}$ of the whole.</p>  <p>$\frac{1}{4}$ of 12 apples is 3 apples.</p>	<p>One ... of ... is ...</p> <p>$\frac{1}{4}$ of 12 is 3</p>  <p>$\frac{1}{3}$ of 36 is 12</p> 																																				

Progression of skills	Key representations	
<p>Non-unit fractions of a set of objects</p> <p>Bar models are a useful representation and show the links with division and multiplication.</p>	<p>The whole is divided into ... equal parts. Each part is $\frac{1}{\square}$ of the whole.</p>  <p>$\frac{3}{4}$ of 12 apples is 9 apples.</p>	<p>$\frac{1}{\square}$ of ... is ..., so $\frac{\square}{\square}$ of ... is ...</p> <p>$\frac{3}{4}$ of 12 is 9 </p> <p>$\frac{2}{3}$ of 36 is 24 </p>

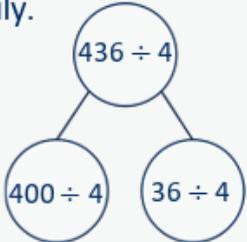
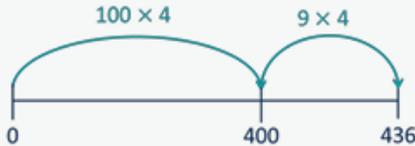
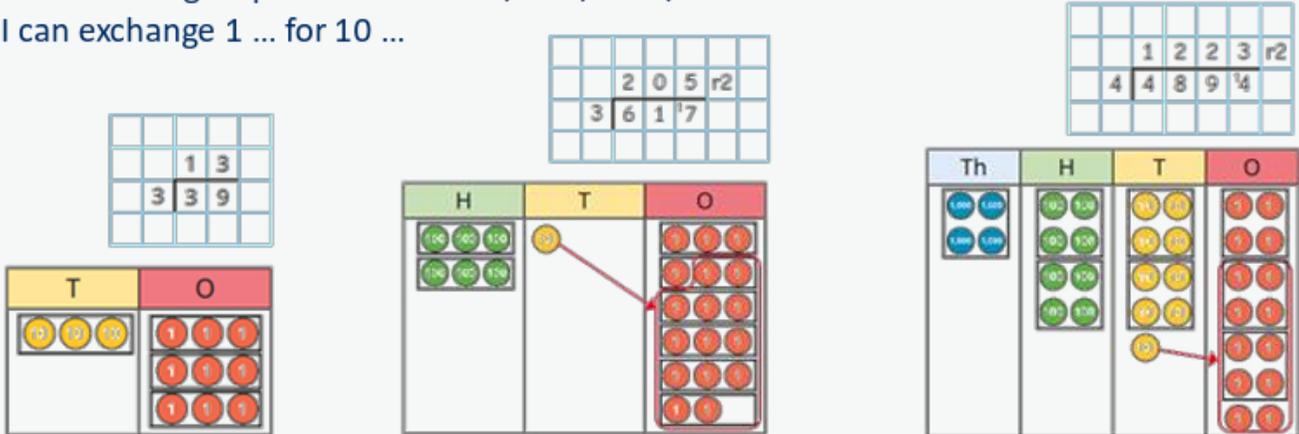
Division - Year 4

<p>Year 4</p>	<ul style="list-style-type: none"> Recall division facts for multiplication tables up to 12×12 Use place value, known and derived facts to divide mentally, including: dividing by 1 Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths. 	
<p>Progression of skills</p>	<p>Key representations</p>	
<p>Division facts to 12×12</p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... groups of ... in ...</p> <p>$\dots \div \dots =$</p>  <p>$2 \times 6 = 12$ $12 \div 6 = 2$</p>	<p>... has been shared equally into ... equal groups.</p> <p>$\dots \div \dots =$</p>  <p>$2 \times 6 = 12$ $12 \div 6 = 2$</p>
<p>Divide a number by 1 and itself</p> <p>Children may try to divide a number by zero and it should be highlighted that this is not possible.</p>	<p>When I divide a number by 1, the number remains the same.</p> <p>5 shared between 1 is 5 </p> <p>There are 5 groups of 1 in 5</p> 	<p>When I divide a number by itself, the answer is 1</p> <p>5 shared between 5 is 1</p>  <p>There is 1 group of 5 in 5</p> 

Progression of skills	Key representations																										
<p>Related facts</p> <p>Link to known times-table facts.</p>	<p>... ÷ ... is equal to ... so ... tens ÷ ... is equal to ... tens and ... hundreds ÷ ... is equal to ... hundreds.</p>  <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> $21 \div 7 = 3$ $210 \div 7 = 30$ $2,100 \div 7 = 300$ </div> <div style="text-align: center;"> $21 \div 3 = 7$ $210 \div 3 = 70$ $2,100 \div 3 = 700$ </div> </div>																										
<p>Divide a 2 or 3-digit number by a 1-digit number</p> <p>Progress from divisions with no exchange, to divisions with exchange and then divisions with remainders.</p>	<p>I can partition ... into ... tens and ... ones.</p>  <div style="display: flex; align-items: center; margin-left: 100px;"> <div style="margin-right: 20px;"> $80 \div 4 = 20$ $4 \div 4 = 1$ $84 \div 4 = 21$ </div> </div> <table border="1" style="margin-top: 10px; width: 100px; text-align: center;"> <thead> <tr> <th style="background-color: #fff9c4;">Tens</th> <th style="background-color: #f8bbd0;">Ones</th> </tr> </thead> <tbody> <tr><td>10 10</td><td>1</td></tr> <tr><td>10 10</td><td>1</td></tr> <tr><td>10 10</td><td>1</td></tr> <tr><td>10 10</td><td>1</td></tr> </tbody> </table>	Tens	Ones	10 10	1	10 10	1	10 10	1	10 10	1	<p>I cannot share the hundreds/tens equally, so I need to exchange 1 ... for 10 ...</p>  <div style="display: flex; align-items: center; margin-left: 100px;"> <div style="margin-right: 20px;"> $300 \div 3 = 100$ $120 \div 3 = 40$ $15 \div 3 = 5$ $435 \div 3 = 145$ </div> </div> <table border="1" style="margin-top: 10px; width: 200px; text-align: center;"> <thead> <tr> <th style="background-color: #c8e6c9;">Hundreds</th> <th style="background-color: #fff9c4;">Tens</th> <th style="background-color: #f8bbd0;">Ones</th> </tr> </thead> <tbody> <tr> <td>100</td> <td>10 10 10 10</td> <td>1 1 1 1 1</td> </tr> <tr> <td>100</td> <td>10 10 10 10</td> <td>1 1 1 1 1</td> </tr> <tr> <td>100</td> <td>10 10 10 10</td> <td>1 1 1 1 1</td> </tr> <tr> <td>100</td> <td>10 10 10 10</td> <td>1 1 1 1 1</td> </tr> </tbody> </table>	Hundreds	Tens	Ones	100	10 10 10 10	1 1 1 1 1	100	10 10 10 10	1 1 1 1 1	100	10 10 10 10	1 1 1 1 1	100	10 10 10 10	1 1 1 1 1
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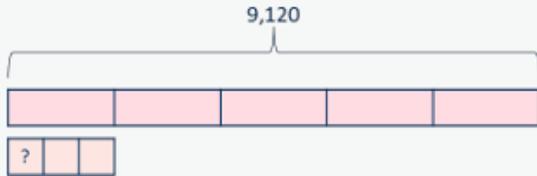
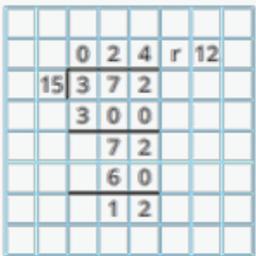
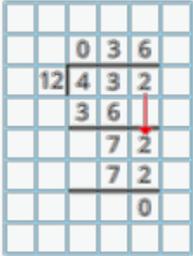
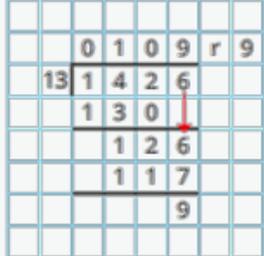
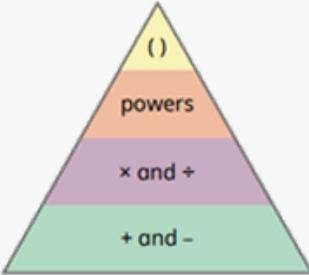
Progression of skills	Key representations			
<p>Divide by 10 and 100</p> <p>Encourage children to notice that dividing by 100 is the same as dividing by 10 twice.</p>	<p>When I divide by 10, the digits move 1 place value column to the right. ... is one-tenth the size of ...</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  <p>$2 \div 10 = 0.2$</p> </div> <div style="text-align: center;">  <p>$12 \div 10 = 1.2$</p> </div> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div>		<p>When I divide by 100, the digits move 2 place value columns to the right. ... is one-hundredth the size of ...</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  <p>$2 \div 100 = 0.02$</p> </div> <div style="text-align: center;">  <p>$12 \div 100 = 0.12$</p> </div> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div>	

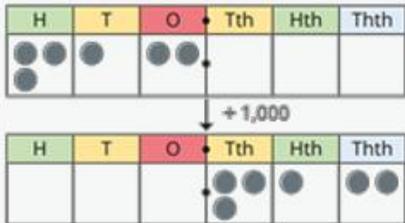
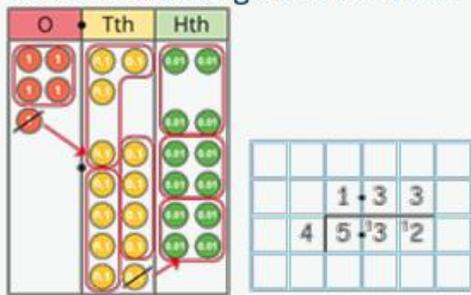
Division - Year 5

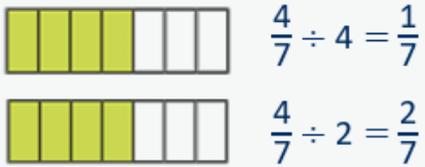
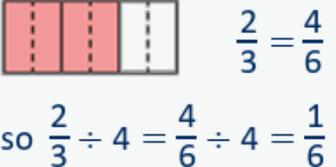
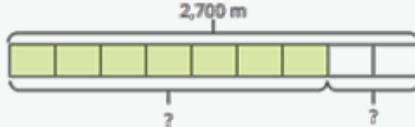
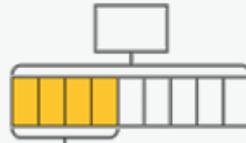
<p>Year 5</p>	<ul style="list-style-type: none"> • Divide numbers mentally drawing upon known facts. • Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context. • Divide whole numbers and those involving decimals by 10, 100 and 1,000 		
<p>Progression of skills</p>	<p>Key representations</p>		
<p>Mental strategies</p>	<p>I can partition ... into ... and ... to help me to divide more easily.</p> 	<p>I can show groups of ... on a number line.</p> 	<p>To divide by ..., I can divide by ... and then divide the result by ...</p> $436 \div 4 = 436 \div 2 \div 2$ $436 \div 2 = 218$ $218 \div 2 = 109$
<p>Divide numbers up to 4 digits by a 1-digit number</p> <p>The short division method is introduced for the first time.</p>	<p>There are ... groups of ... hundreds/tens/ones/ in ... I can exchange 1 ... for 10 ...</p> 		

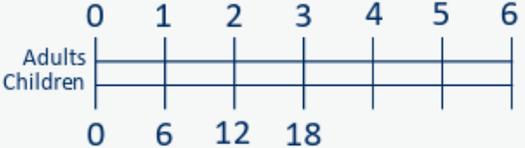
Progression of skills	Key representations																																																	
<p>Divide by 10, 100 and 1,000</p> <p>Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.</p>	<p>To divide by 10/100/1,000, I move all the digits ... places to the right. ... is one-tenth/one-hundredth/one-thousandth the size of ...</p> <table border="1" data-bbox="683 327 1097 422"> <tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr> <tr><td></td><td>●</td><td>●●</td><td>●</td><td>●</td><td></td></tr> </table> <p data-bbox="1131 462 1355 494">$120 \div 10 = 12$</p> <table border="1" data-bbox="683 430 1097 526"> <tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr> <tr><td></td><td></td><td>●</td><td>●●</td><td>●</td><td></td></tr> </table> <p data-bbox="1131 566 1377 598">$120 \div 100 = 1.2$</p> <table border="1" data-bbox="683 542 1097 630"> <tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr> <tr><td></td><td></td><td></td><td>●</td><td>●●</td><td>●</td></tr> </table> <p data-bbox="1131 678 1422 710">$120 \div 1,000 = 0.12$</p> <table border="1" data-bbox="683 638 1097 734"> <tr><th>Th</th><th>H</th><th>T</th><th>O</th><th>Tth</th><th>Hth</th></tr> <tr><td></td><td></td><td></td><td>●</td><td>●</td><td>●●</td></tr> </table>		Th	H	T	O	Tth	Hth		●	●●	●	●		Th	H	T	O	Tth	Hth			●	●●	●		Th	H	T	O	Tth	Hth				●	●●	●	Th	H	T	O	Tth	Hth				●	●	●●
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<p>Fraction of an amount</p> <p>Bar models support children to understand that to find a fraction of an amount, we divide by the denominator and multiply by the numerator.</p>	<p>To find $\frac{\square}{\square}$ of ... , I need to divide by ... and multiply by ...</p> <table border="1" data-bbox="683 893 1052 973"> <tr><td>●●</td><td>●●</td><td>●●</td><td>●●</td><td>●●</td></tr> <tr><td>●●</td><td>●●</td><td>●●</td><td>●●</td><td>●●</td></tr> </table> <table border="1" data-bbox="1075 893 1388 973"> <tr><td>●●</td><td>●●</td><td>●●</td><td>●●</td><td>●●</td></tr> <tr><td>●</td><td>●</td><td>●</td><td>●</td><td>●</td></tr> </table> <p data-bbox="683 1013 840 1093">$\frac{1}{5}$ of 20 =</p> <p data-bbox="1086 1013 1243 1093">$\frac{1}{4}$ of 84 =</p> <p data-bbox="683 1117 840 1197">$\frac{3}{5}$ of 20 =</p> <p data-bbox="1086 1117 1243 1197">$\frac{3}{4}$ of 84 =</p>	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●●	●	●	●	●	●	<p>If $\frac{1}{\square}$ is ... , then the whole is ... \times ...</p> <table border="1" data-bbox="1433 829 1724 965"> <tr><td colspan="5">?</td></tr> <tr><td>6</td><td>6</td><td>6</td><td>6</td><td>6</td></tr> </table> <p data-bbox="1814 893 2004 965">$\frac{1}{5}$ of ___ = 6</p> <table border="1" data-bbox="1433 997 1758 1181"> <tr><td colspan="7">?</td></tr> <tr><td colspan="3">24</td><td></td><td></td><td></td><td></td></tr> </table> <p data-bbox="1803 1053 2004 1125">$\frac{4}{7}$ of ___ = 24</p>	?					6	6	6	6	6	?							24										
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Division - Year 6

Progression of skills	Key representations	
<p>Mental strategies</p> <p>Include partitioning and number line strategies outlined in Y5 as well as division using factors.</p>	<p>To divide by ... , I can first divide by ... and then divide the answer by ...</p> <p> $240 \div 60 = 240 \div 10 \div 6$ $240 \rightarrow \xrightarrow{+10} \square \rightarrow \xrightarrow{+6} \square$ </p> <p> $480 \div 24 = 480 \div 4 \div 6$ $480 \rightarrow \xrightarrow{+4} \square \rightarrow \xrightarrow{+6} \square$ </p> <p> $9,120 \div 15 = 9,120 \div 5 \div 3$ </p> 	
<p>Long division</p> <p>The long division method is introduced for the first time. Two alternative methods are shown.</p>	<p>Method 1</p>  <p>(12×30)</p>  <p>(15×20)</p> <p>(15×4)</p>	<p>Method 2</p>  
<p>Order of operations</p> <p>Calculations in brackets should be done first, then powers. Multiplication and division should be performed before addition and subtraction.</p>	<p>... has greater priority than ..., so the first part of the calculation I need to do is ...</p>  <p>  $(6 + 4) \div 2 = 5$ </p> <p>  $6 + 4 \div 2 = 8$ </p>	

Progression of skills	Key representations																																									
<p>Divide by 10, 100 and 1,000</p> <p>Encourage children to notice that dividing by 100 is the same as dividing by 10 twice, and that dividing by 1,000 is the same as dividing by 10 three times.</p>	<p>To divide by ... , I move the digits ... places to the right.</p>  <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <div style="text-align: center;"> $312 \div 10 = 31.2$ $312 \div 100 = 3.12$ $312 \div 1,000 = 0.312$ </div> <div style="text-align: center;"> $906 \div 10 = 90.6$ $906 \div 100 = 9.06$ $906 \div 1,000 = 0.906$ </div> </div>																																									
<p>Divide decimals by integers</p> <p>This is the first time children divide decimals by numbers other than 10, 100 or 1,000</p>	<p>I know that ... \div ... = ..., so I also know that ... \div ... = ...</p> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 10px;"> <div style="text-align: center;">  $39 \div 3 = 13$ </div> <div style="text-align: center;">  $3.9 \div 3 = 1.3$ </div> <div style="text-align: center;">  $0.39 \div 3 = 0.13$ </div> </div>	<p>I need to exchange 1 ... for 10 ...</p> 																																								
<p>Decimal and fraction equivalents</p>	<p>The fraction ... is equivalent to the decimal ...</p> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td colspan="4" style="background-color: #d9ead3;">1</td></tr> <tr><td colspan="2" style="background-color: #f4cccc;">1/2</td><td colspan="2" style="background-color: #f4cccc;">1/2</td></tr> <tr><td colspan="1" style="background-color: #fff2cc;">1/4</td><td colspan="1" style="background-color: #fff2cc;">1/4</td><td colspan="1" style="background-color: #fff2cc;">1/4</td><td colspan="1" style="background-color: #fff2cc;">1/4</td></tr> <tr><td colspan="1" style="background-color: #d9ead3;">1/5</td><td colspan="1" style="background-color: #d9ead3;">1/5</td><td colspan="1" style="background-color: #d9ead3;">1/5</td><td colspan="1" style="background-color: #d9ead3;">1/5</td></tr> <tr><td colspan="1" style="background-color: #d9ead3;">1/10</td><td colspan="1" style="background-color: #d9ead3;">1/10</td><td colspan="1" style="background-color: #d9ead3;">1/10</td><td colspan="1" style="background-color: #d9ead3;">1/10</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td colspan="4" style="background-color: #d9ead3;">1</td></tr> <tr><td colspan="2" style="background-color: #fff2cc;">0.5</td><td colspan="2" style="background-color: #fff2cc;">0.5</td></tr> <tr><td colspan="1" style="background-color: #fff2cc;">0.25</td><td colspan="1" style="background-color: #fff2cc;">0.25</td><td colspan="1" style="background-color: #fff2cc;">0.25</td><td colspan="1" style="background-color: #fff2cc;">0.25</td></tr> <tr><td colspan="1" style="background-color: #d9ead3;">0.2</td><td colspan="1" style="background-color: #d9ead3;">0.2</td><td colspan="1" style="background-color: #d9ead3;">0.2</td><td colspan="1" style="background-color: #d9ead3;">0.2</td></tr> <tr><td colspan="1" style="background-color: #d9ead3;">0.1</td><td colspan="1" style="background-color: #d9ead3;">0.1</td><td colspan="1" style="background-color: #d9ead3;">0.1</td><td colspan="1" style="background-color: #d9ead3;">0.1</td></tr> </table> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <div style="text-align: center;">$\frac{1}{5} = 0.2$</div> <div style="text-align: center;">$\frac{2}{5} = 0.4$</div> <div style="text-align: center;">$\frac{3}{5} = 0.6$</div> </div> <div style="margin-top: 20px;"> <p>$\frac{\square}{\square}$ is equal to $\frac{\square}{100}$</p> <div style="text-align: center; margin-top: 10px;"> $\frac{3}{4} \xrightarrow{\times 25} \frac{75}{100} = 0.75$ </div> </div>		1				1/2		1/2		1/4	1/4	1/4	1/4	1/5	1/5	1/5	1/5	1/10	1/10	1/10	1/10	1				0.5		0.5		0.25	0.25	0.25	0.25	0.2	0.2	0.2	0.2	0.1	0.1	0.1	0.1
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Progression of skills	Key representations		
<p>Divide a fraction by an integer</p> <p>This is the first time children divide fractions by an integer.</p>	<p>... ones divided by 2 is ... ones so ... sevenths divided by 2 is ... sevenths.</p> 	<p>I am dividing by ... , so I can split each part into ... equal parts.</p> 	<p>... is equivalent to ... so ... ÷ ... = ... ÷ ...</p> 
<p>Fraction of an amount</p> <p>Children divide and multiply to find fractions of an amount. Bar models can still be used to support understanding where needed.</p>	<p>To find $\frac{1}{\square}$ I divide by ...</p> <p>$\frac{1}{2}$ of 36 = $36 \div 2$</p> <p>$\frac{1}{12}$ of 36 = $36 \div 12$</p>	<p>If $\frac{1}{\square}$ is equal to ..., then $\frac{\square}{\square}$ are equal to ...</p>  <p>$\frac{7}{9}$ of 2,700 = $\frac{1}{9}$ of 2,700 $\times 7$</p>	<p>If $\frac{\square}{\square}$ is equal to ..., then the whole is equal to ...</p>  <p>$\frac{4}{9}$ of ___ = 48</p>

Progression of skills	Key representations																																	
<p>Calculate percentages</p> <p>Children first learn how to find 1%, 10%, 20%, 25% and 50% before using multiples of these amounts to find any percentage.</p>	<p>There are ... lots of ... % in 100%</p> <p>To find ... %, I need to divide by ...</p> <table border="1" data-bbox="680 312 1178 424"> <tr><td colspan="4">100%</td></tr> <tr><td colspan="2">50%</td><td colspan="2">50%</td></tr> <tr><td>25%</td><td>25%</td><td>25%</td><td>25%</td></tr> </table> <p>50% of ... = ... ÷ 2</p> <p>25% of ... = ... ÷ 4</p>	100%				50%		50%		25%	25%	25%	25%	<p>... % is made up of ... %, and ... %</p> <table border="1" data-bbox="1240 296 1989 389"> <tr><td colspan="10">100%</td></tr> <tr><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td><td>10%</td></tr> </table> <p>To find 30%, I can find 10% and then multiply it by 3</p> <p>To find 23%, I can use 10% × 2 and 1% × 3</p> <p>To find 99%, I can find 1%, then subtract from 100%</p>	100%										10%	10%	10%	10%	10%	10%	10%	10%	10%	10%
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<p>Calculations involving ratio</p> <p>Encourage children to see the multiplicative relationship between ratios. They will need to multiply or divide each value by the same number to keep the ratio equivalent. Double number lines and ratio tables help children to see both horizontal and vertical multiplicative relationships.</p>	<p>For every ... , there are ...</p> <p>For every 6 children on a school trip, there is 1 adult.</p> <p>adults </p> <p>children </p> <table border="1" data-bbox="1585 703 1906 895"> <thead> <tr><th>Adults</th><th>Children</th></tr> </thead> <tbody> <tr><td>1</td><td>6</td></tr> <tr><td>2</td><td>12</td></tr> <tr><td>3</td><td>18</td></tr> </tbody> </table> <p>The ratio of children to adults is 6 : 1</p> 		Adults	Children	1	6	2	12	3	18																								
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